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MODELLING AND SIMULATION OF A BIOMASS GASIFICATION-SOLID OXIDE FUEL CELL COMBINED HEAT AND POWER PLANT USING ASPEN PLUS

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Abstract. In this paper the operation and performance of a high temperature solid oxide fuel cell (SOFC) stack on biomass syn-gas from a demonstration biomass gasification combined heat and power (CHP) plant is investigated. The objective of this work is to develop a computer simulation model of a biomass-SOFC CHP system, flexible enough for use in industry, capable of predicting system performance under various operating conditions and using diverse fuels. The biomass gasifier is of the dual fluidised bed (DFB) type with steam as the gasifying agent and is operated at atmospheric pressure. The tubular SOFC configuration, developed by Siemens Power Generation Inc (SPGI), is selected. It is considered to be the most advanced design and is approaching commercialisation. The SOFC stack model, developed using the chemical process flowsheet simulator Aspen Plus, is of equilibrium type and is based on Gibbs free energy minimisation. The SOFC model performs heat and mass balances and considers the ohmic, activation and concentration losses for the voltage calculation. Data available in the literature on the SPGI SOFC operating on natural gas is used to validate the model. The system model predicts thermodynamic condition and composition of all internal flow streams, the heat generated by the SOFC stack, voltage (V), current (I) and efficiency. Operating parameters are varied over a wide range, parameters such as fuel utilisation factor (Uf), current density (j) and steam to carbon ratio (STCR) have significant influence. The results indicate that there must be a trade-off between voltage, efficiency and power with respect to j and the SOFC stack should be operated at low STCR and high Uf within certain limits. SOFC stack operation on biomass syn-gas is compared to operation on natural gas and as expected there is a drop in performance, which is attributed to increased input fuel and air flow due to the lower quality of the fuel gas. The optimum realistic operating conditions with regard to SOFC stack performance are identified. High electrical efficiencies are predicted making these systems very attractive for CHP applications.

Keywords: biomass gasification, fuel cell, computer simulation, Gibbs free energy, model validation

1. INTRODUCTION

Biomass is among the most promising renewable energy sources in the context of both climate change mitigation and energy security. Energy is primarily recovered from biomass through combustion at low electrical efficiency, typically 20-25%. Biomass gasification coupled with advanced power generation technologies such as micro gas turbines and fuel cells offer much higher efficiencies. Reported electrical efficiencies (predicted) for biomass gasification-solid oxide fuel cell (SOFC) systems range from 23-50% (Seitarides et al. 2008). These systems offer highly efficient renewable energy and are modular in nature making them ideal for decentralised combined heat and power (CHP) applications and as a result have recently gained much attention (Pröll et al. 2004, Panopoulos et al. 2006, Cordiner et al. 2007, Sucipta et al. 2007, Suwanwarangkul et al. 2007, Fryda et al. 2008, Sucipta et al. 2008, Toonssen et al. 2008). Decentralised CHP is appropriate for biomass energy conversion systems as there may be major logistical problems regarding the availability of the fuel for large centralised plants.

Gasification occurs when a controlled amount of oxidant (pure oxygen (O2), air, steam) is reacted at high temperatures with available carbon in biomass or other carbonaceous material within a gasifier, producing a combustible gas commonly known as syn-gas. Biomass syn-gas typically contains hydrogen (H2), carbon monoxide (CO), methane (CH4), carbon dioxide (CO2), water (H2O), nitrogen (N2) and other components such as higher hydrocarbons. Air gasification produces a poor quality gas with regard to heating value, around 4-7 MJ/m3 higher heating value (HHV), while O2 and steam blown processes result in a syn-gas with a heating value in the range of 10-18 MJ/m3 (HHV) (Schuster et al. 2001). Recently, Sucipta et al. (2007) found that biomass-SOFC systems achieved higher efficiencies when steam is used compared to pure O2 or air. This is due to the higher heating value of the gas and the fact that the syn-gas is not diluted with N2 and has high H2 content. Atmospheric pressure fluidised bed gasification technology has been proven to operate effectively with many biomass fuels. These gasifiers have potential for scale-up from low MW to over 100 MW and possess high fuel flexibility, which is of utmost importance for biomass gasification plants as biomass fuels can be seasonal. Considering all of the above, the dual fluidised bed (DFB) steam gasification technology, also known as fast internally circulating fluidised bed (FICFB), was selected for this study. This technology is currently in operation at the Güssing demonstration CHP plant in Austria.
The SOFC is a highly efficient energy conversion device due to the fact that it converts the chemical energy contained in a fuel gas directly to electrical energy by means of electrochemical reactions. SOFCs are considered one of the most promising energy conversion devices since they can achieve very high electrical efficiencies with low emissions and good reliability (Calise et al. 2008). They can utilise a wide spectrum of fuels (natural gas, coal and biomass syn-gas) due to its high operating temperature, which also makes them suitable for integration with gas turbines and for cogeneration. The tubular SOFC configuration, developed by Siemens Power Generation Inc (SPGI) formerly Siemens-Westinghouse, is considered to be the most advanced and is approaching commercialisation, therefore it was selected for this study. Various models have been developed previously to simulate tubular SOFC performance, many of them for operation on humidified H₂ or natural gas (Bessette et al. 1995, Campanari, 2001, Campanari and Iora, 2004, Bharadwaj et al. 2005, Cali et al. 2007). A review of SOFC models, including those for planar and monolithic designs, can be found in the literature (Kakaç et al. 2007).

An advantage of the tubular SOFC is that it operates at a similar temperature to the biomass gasifier (800 – 1000 °C), making heat integration possible. Heat integration is attractive for steam gasification as it is an endothermic process. Recently, Athanasiou et al. (In Press) reported that the SOFC heat is sufficient to cover the requirements of the gasification process and syn-gas reforming with excess heat for a bottoming cycle. This will be investigated in a future study.

There is a need for SOFC models that are easily calibrated to match the continuous and rapid technological advances in the field. Also the models should have short computational times. In the present study the operation and performance of a tubular SOFC stack (SPGI design) on biomass syn-gas was investigated. The objective of this work was to develop a computer simulation model of a biomass-SOFC CHP system, flexible enough for use in industry, capable of predicting system performance under various operating conditions and using diverse fuels.

Aspen Plus, which is widely used in industry, was used to model the SOFC stack. There is no built in model that can represent a SOFC. A common approach is to develop a complete SOFC stack model in a programming language and link it to Aspen Plus as a subroutine (Zhang et al. 2005). The subroutine must incorporate complex phenomena such as chemical/electrochemical reactions and heat and mass transfer, making them difficult and time consuming to develop and use. This type of model would not achieve the objectives of this work. An alternative method proposed by Zhang et al. (2005), using existing Aspen Plus unit operation blocks with minimum requirements for linking of a subroutine was used. The equilibrium model, which is based on Gibbs free energy minimisation, performs heat and mass balances and considers the ohmic, activation and concentration losses for the voltage calculation. Equations reported by Song et al. (2005) were used to calculate ohmic loss, taking into account realistic electron/ion paths. Achenbach’s semi-empirical correlations were implemented to determine the activation loss (Achenbach, 1994). Both ordinary and Knudsen diffusion were considered for the calculation of effective diffusion coefficients and the equations derived by Chan et al. (2001) were used for the calculation of the concentration loss.

2. TECHNOLOGY DESCRIPTION

2.1. Güssing biomass CHP plant

The Güssing biomass CHP plant has been in operation since 2001 and utilises 8 MW of wood chip fuel to produce 2 MWₜ of electricity (grid connected) by means of a gas engine and 4.5 MWₜ of heat (connected to the local district heating system). The biomass syn-gas is produced using a DFB steam gasifier. This type of gasifier operates with two separate zones, the combustion zone and the gasification zone. Residual char is combusted with air in the combustion zone and the heat is transferred to the gasification zone via circulating bed material. This heat drives the endothermic steam gasification reactions which produce the syn-gas. A more detailed description of the process can be found in the literature (Schuster et al. 2001, Pröll et al. 2004). Efforts are ongoing to get a SOFC stack installed for testing at the Güssing plant (Pröll, 2008). The following syn-gas composition was inputted to the SOFC stack model: 45.8% H₂, 21.6% CO, 10.0% CH₄, 21.2% CO₂, 1.4% N₂ (volume %, dry basis) and 25.7% H₂O (volume %, wet basis) (Pröll et al. 2004). This syn-gas composition is typical of the Güssing DFB gasifier operating at 850 °C with a steam/fuel ratio of 0.75 and after gas cleaning.

2.2. SPGI 100 kW CHP SOFC stack

The 100 kW AC CHP tubular SOFC stack developed by SPGI was selected and modelled. It was the first field unit to utilise the seal-less cathode supported cell (22 mm diameter, 150 cm active length, 834 cm² active area) and in stack reformers (George, 2000). This unit was operated on natural gas for over 20,000 hours in the Netherlands and Germany and provided 108 kW AC electricity and 85 kW of hot water for district heating at an AC efficiency of 47% (LHV) (Williams et al. 2004). This unit is currently installed at Gas Turbine Technologies in Torino, Italy and has been operated for a further 16,000 hours (Gariglio et al. In Press). It employs 1152 cells in 48 bundles of 24 cells each (Williams et al. 2004). The operation of this system is as follows:
The oxidant stream is fed via injector tubes, placed centrally in each SOFC, to the closed end of the cells. The oxidant then flows back through the annular space formed by the cathode surface and the injector tube to the open end. The oxidant is electrochemically reacted with the fuel supplied to the anode as it flows over the cathode surface. Cleaned fuel gas at sufficient pressure is supplied to the ejector where it is mixed with depleted fuel from the recirculation plenum. This anode recycle loop provides the steam and heat required for the steam reforming process. The mixed fuel then passes through the pre-reformers which convert the higher hydrocarbons and a small portion of the $\text{CH}_4$ adiabatically to $\text{H}_2$ and CO. The partially reformed fuel enters the internal reformers and using the heat generated by the exothermic electrochemical reactions occurring in the SOFC stack it is reformed further. The fuel then flows along the anode surface from the closed end to the open end, parallel to the direction of the oxidant flow and is electrochemically oxidised, generating electricity and increasing the temperature of both streams. A portion of the depleted fuel is recycled, the quantity of which depends on the required $STCR$ and the remainder is reacted with the depleted oxidant in the combustion plenum. The generated heat serves to preheat the incoming oxidant stream in the injector tubes. The high temperature exhaust gas may then be utilised in a district heating system.

3. MODELLING

3.1. Aspen Plus flowsheet

Figure 1 depicts the Aspen Plus flowsheet of the SOFC stack.

![Aspen Plus flowsheet](image)

Figure 1. SOFC stack model Aspen Plus flowsheet

3.2. Model description

3.2.1. Flowsheet description

With reference to Fig. 1, the stream ‘SYN-GAS’ is fed to the ‘COMP1’ block, simulating the fuel compressor. The discharge pressure was calculated by assuming a pressure ratio: $P_{\text{fuel}}/P_{\text{SOFC}} = 3$ (Campanari, 2001). The syn-gas stream composition and thermodynamic condition were inputted; its mole flow rate is set by a design spec and depends on the specified stack power (or for variable power a calculator block sets the mole flow depending on the specified $j$). The pressurised fuel is brought up to the fuel preheat temperature in the block ‘FUELHEAT’ and its exit stream enters the ‘EJECTOR’ block, where it is mixed with the recycled depleted fuel (stream 8). The pressure of the mixed stream (stream 4) is decreased back to slightly above atmospheric pressure ($P_{\text{SOFC}}$) and is directed to the ‘COOLER1’ block. The two blocks ‘COOLER1’ and ‘PREREFOR’ simulate the operation of the pre-reformers. The purpose of ‘COOLER1’ is to set the pre-reforming temperature. It is calculated by means of a design spec, which varies the temperature of ‘COOLER1’ until the net heat duty of ‘PREREFOR’ equals zero (adiabatic). As a result, the gas is cooled simulating the endothermicity of the steam reforming process. The following chemical reactions were specified in the ‘PREREFOR’ block:
Steam reforming: \[ \text{C}_n\text{H}_m + n\text{H}_2\text{O} \leftrightarrow (m/2 + n) \text{H}_2 + n\text{CO} \quad (1) \]
Water-gas shift: \[ \text{CO} + \text{H}_2\text{O} \leftrightarrow \text{CO}_2 + \text{H}_2 \quad (2) \]

It was assumed that the reactions reach thermodynamic equilibrium at the pre-reforming temperature. The reader should note that it is possible that the reverse water-gas shift reaction is favoured at the high temperatures occurring in the SOFC stack. The pre-reformed fuel (stream 6) is fed to the ‘ANODE’ block, where the remaining CH\textsubscript{4} is reformed, CO is shifted and H\textsubscript{2} is oxidised. In a SOFC the following reactions occur:

- Cathode half reaction: \[ 0.5\text{O}_2 + 2e^- \rightarrow \text{O}^2- \quad (3) \]
- Anode half reaction: \[ \text{H}_2 + \text{O}^2- \rightarrow \text{H}_2\text{O} + 2e^- \quad (4) \]
- Overall reaction: \[ \text{H}_2 + 0.5\text{O}_2 \rightarrow \text{H}_2\text{O} \quad (5) \]

The oxygen ion O\textsuperscript{2-} is the charge carrier in a SOFC. It is transported through the electrolyte to the anode side where it reacts with H\textsubscript{2} to produce electrons e\textsuperscript{-}. The transfer of ions cannot be modelled in Aspen Plus; therefore the overall reaction of the cell half reactions was used in the simulation. Although it is possible to directly oxidise CH\textsubscript{4} and CO in a SOFC at its high operating temperature, it is common to assume that the CH\textsubscript{4} is reformed and the CO is shifted to H\textsubscript{2} and therefore only H\textsubscript{2} participates in the electrochemical reaction. Reactions (1), (2) and (5) were specified in the ‘ANODE’ block and it was assumed that they reach thermodynamic equilibrium at the block temperature (\(T_{\text{op}} = 910 \) °C). The oxidant (stream ‘AIR’) is fed to the ‘COMP2’ block, the air compressor. Its discharge pressure was set as slightly above atmospheric pressure (\(P_{\text{SOFC}}\)). The air stream composition and thermodynamic condition were inputted.

The molar flow rate is determined using a design spec that varies the air flow until the air utilisation factor \(U_a = 16.7\%\) (Suwanwarangkul et al. 2007). The compressed air is brought up to the air preheat temperature in the block ‘AIRHEAT’ and its exit stream enters ‘HEATX1’ where it is preheated further by the hot combustion plenum products. The compressed and preheated air (stream 15) enters the ‘CATHODE’ block, whose function is to separate out the O\textsuperscript{2-} required for the electrochemical reaction (nO\textsubscript{2,consumed}). The ‘CATHODE’ block O\textsubscript{2} split fraction is set by a calculator block using the following equations: \[ U_j = n\text{H}_2\text{consumed}/n\text{H}_2\text{in} \] where \(n\text{H}_2\text{consumed}\) is calculated, \(n\text{O}_2\text{,consumed} = 0.5n\text{H}_2\text{,consumed}\) and O\textsubscript{2} split fraction = \(n\text{O}_2\text{,consumed}/n\text{O}_2\text{,in}\). It is worth noting that the O\textsubscript{2} split fraction is equivalent to \(U_j\). A typical value for \(U_j\) is 0.85. The \(n\text{H}_2\text{,in}\) term is calculated as follows: \[ n\text{H}_2\text{,in} = n\text{H}_2\text{,syn-gas} + 1(n\text{CO}_2\text{,syn-gas}) + 4(n\text{CH}_4\text{,syn-gas}) + 7(n\text{C}_2\text{H}_6\text{,syn-gas}) + \ldots \] where \(n\text{H}_2\text{,syn-gas}\) represents the molar flow rate of H\textsubscript{2} contained in the stream ‘SYN-GAS’; \(1(n\text{CO}_2\text{,syn-gas})\) represents the molar flow rate of H\textsubscript{2} that could be produced from the CO contained in ‘SYN-GAS’; \(4(n\text{CH}_4\text{,syn-gas})\) represents the molar flow rate of H\textsubscript{2} that could be produced from the CH\textsubscript{4} in ‘SYN-GAS’ and the same applies to the higher hydrocarbons. Following the O\textsubscript{2} split calculation the required O\textsubscript{2} is directed to the ‘ANODE’ block (stream 16). The temperature of the depleted air (stream 17) must be increased to the stack operating temperature (\(T_{\text{op}}\)). The heat needed to do this is supplied by the electrochemical reaction and this process was simulated by taking a heat stream (Q\textsubscript{3}) from ‘HEATER2’ to ‘ANODE’. The temperature of the ‘HEATER2’ block was specified as 910 °C (\(T_{\text{op}}\)). The depleted fuel (stream 7) enters the block ‘SPLIT’, whose function is to split the stream into a recycle (stream 8) and a stream directed to the combustion plenum. The split fraction of the block is set using a design spec where it is determined by a specified STCR, defined as the molar ratio of steam to combustible carbon, a typical value being 2.5. Excess steam as well as increasing the concentration of H\textsubscript{2} and CO\textsubscript{2} inhibits the formation of carbon. Carbon deposition not only represents a loss in the system but results in deactivation of catalysts and decreases the activity of the anode by clogging the active sites. The depleted fuel and oxidant are fed to ‘POSTCOMB’ where complete combustion of the remaining fuel occurs. The following combustion reactions, assumed to reach completion, were specified:

- H\textsubscript{2} combustion: \[ \text{H}_2 + 0.5\text{O}_2 \rightarrow \text{H}_2\text{O} \quad (6) \]
- CO combustion: \[ \text{CO} + 0.5\text{O}_2 \rightarrow \text{CO}_2 \quad (7) \]
- CH\textsubscript{4} combustion: \[ \text{CH}_4 + 2\text{O}_2 \rightarrow \text{CO}_2 + 2\text{H}_2\text{O} \quad (8) \]

The heat generated by the reactions is calculated and is put into the heat stream Q\textsubscript{5}, which is fed to the block ‘HEATER1’, whose function is to calculate and set the combustion products temperature. Finally, the high temperature combustion products (stream 11) exchange heat with and serve to preheat the incoming air in the ‘HEATX1’ block. The temperature of the SOFC stack exhaust (stream 12), which may be utilised in a district heating system, is also determined.

### 3.2.2. Voltage calculation

The voltage was calculated by first applying the widely known Nernst equation, Eq. (9) Tab. 1, to determine the reversible Nernst voltage \(V_n\) and then subtracting the various losses, including ohmic, activation and concentration losses. In Eq. (9) \(\Delta_f\), is the molar Gibbs free energy of formation (J/mol) at standard pressure (1 bar), 2 represents the number of electrons produced per mole of H\textsubscript{2} fuel reacted, \(F\) is the Faraday constant (96485 C/mol), \(T_{\text{avg}}\) is the average temperature between the SOFC inlet and outlet streams (K), \(R_g\) is the molar gas constant and was taken as 8.314 J/mol.
The ohmic loss, which is the voltage loss due to the resistance to electron flow through both electrodes and the interconnection and the resistance to ion flow through the electrolyte, was calculated using Eq. (10) – (13). These equations developed by Song et al. (2005) take into account realistic electron/ion paths in a tubular SOFC. They assumed uniform current density in the circumferential direction and uniform ionic flux in the electrolyte in the radial direction. The angle related to the extent of electrical contact is $\Lambda \pi$ radians while the angle $B \pi$ radians is related to the interconnection. The equations were developed using Ohm’s law: $V_{\text{ohm,}} = IR$, and the resistivity equation: $R_i = \rho_i(l/A)$, where $\rho_i$ is the material resistivity ($\Omega\ m$), $l$ is the current flow length (m) and $A$ is the area through which the current flows ($m^2$). The resistivity terms were determined using the temperature dependent relations proposed by Bessette et al. (1995), given in Tab. 2. Other terms that appear in Eq. (10) – (13) include $D_{\text{m}}$, which is the mean diameter of a cell (m), calculated from the geometry parameters given in Tab. 2, the cell component thickness $t_i$ (m) and the interconnection width $w_{\text{int}}$ (m). Uniform axial voltage is assumed and also no current transport in the axial direction. The ohmic loss is especially important for tubular SOFCs as it is the dominant loss due to long current flow paths.

### Table 2. Input parameters

<table>
<thead>
<tr>
<th>Geometry parameters (Campanari and Iora, 2004, Williams et al. 2004)</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Cell length (m)</td>
<td>1.5</td>
</tr>
<tr>
<td>Cell outer diameter (m)</td>
<td>0.022</td>
</tr>
<tr>
<td>Anode thickness $t_a$ (m)</td>
<td>0.0001</td>
</tr>
<tr>
<td>Cathode thickness $t_c$ (m)</td>
<td>0.0002</td>
</tr>
<tr>
<td>Electrolyte thickness $t_p$ (m)</td>
<td>0.00004</td>
</tr>
<tr>
<td>Interconnection thickness $t_{\text{int}}$ (m)</td>
<td>0.000085</td>
</tr>
<tr>
<td>Interconnection width $w_{\text{int}}$ (m)</td>
<td>0.009</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Material properties</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Anode resistivity $\rho_a$ ($\Omega\ m$) (Bessette et al. 1995)</td>
<td>$2.98 \times 10^3 \exp(-1392/T_{\text{op}})$</td>
</tr>
<tr>
<td>Cathode resistivity $\rho_c$ ($\Omega\ m$) (Bessette et al. 1995)</td>
<td>$8.114 \times 10^3 \exp(600/T_{\text{eq}})$</td>
</tr>
<tr>
<td>Electrolyte resistivity $\rho_p$ ($\Omega\ m$) (Bessette et al. 1995)</td>
<td>$2.94 \times 10^3 \exp(10350/T_{\text{eq}})$</td>
</tr>
<tr>
<td>Interconnection resistivity $\rho_{\text{int}}$ ($\Omega\ m$) (Campanari and Iora, 2004)</td>
<td>0.025</td>
</tr>
</tbody>
</table>

### Ohmic loss (Song et al. 2005)

| $\Lambda / B$ | 0.804 / 0.13 |
| Activation loss (Achenbach, 1994) |  |
| Pre-exponential factor $k_0 / k_r$ $(A\ m^2)$ | $2.13 \times 10^3 / 1.49 \times 10^4$ |
The activation loss due to slow or sluggish kinetics of the electrochemical reaction taking place on the electrodes was determined using the semi-empirical correlations proposed by Achenbach, (1994) (14) and (15). It is the voltage lost as a result of the energy barrier that must be overcome by the reacting species. In Eq. (14) and (15) the \( R_{\text{act,i}} \) terms represent specific resistance (\( \Omega \cdot \text{m}^2 \)) at both anode and cathode. The activation voltage loss \( V_{\text{act,i}} \) was evaluated by multiplying the specific resistance terms by \( j \) (A/m\(^2\)). The pre-exponential factors \( k_i \), determined experimentally are listed in Tab. 2. The partial pressures \( P_i \) (bar) were taken as average values of the anode and cathode inlet and outlet streams. \( P^0 \) is a reference pressure and was taken as 1 bar; the influence of partial pressure is accounted for by the slope \( m \). The \( E_i \) terms are activation energies and are listed in Tab. 2. The activation voltage loss is less significant in SOFCs compared to other fuel cells due to the high operating temperature.

The concentration loss due to mass transfer limitations in the porous electrodes was modelled using Eq. (16) and (17), which were derived by Chan et al. (2001). Diffusion transport in the electrodes (gases in pores) was considered with convection in the gas channel neglected. The diffusion driving force is the difference in concentration of reactants and products between the reacting sites and the bulk flow, caused by current being drawn from the cell. Equations (16) and (17) were derived using Fick’s law of diffusion and both ordinary and Knudsen diffusion were considered. Ordinary diffusion occurs when the pore diameter of the material is large in comparison to the mean free path of the gas molecules, whereas Knudsen diffusion occurs when the pores are small (Chan et al. 2001). For the Knudsen type the gas molecules are impeded due to frequent collisions with the pore walls. Both types of diffusion were accounted for by calculating effective diffusion coefficients for the anode and cathode. The following equation was used to determine the Knudsen diffusion coefficients for the anode and cathode gases: \( D_{\text{A,K}} = 97\{T_{\text{op}}/M_i\}^{0.7} \) (m\(^2\)/s) where subscripts \( A \) represents the gaseous component (\( \text{H}_2, \text{H}_2 \text{O}, \text{O}_2 \) or \( \text{N}_2 \)), \( r \) is the electrode pore radius (m) and \( M_i \) is the molecular weight (kg/kmol) of the gaseous component. The effective Knudsen diffusion coefficient is given by: \( D_{\text{A,K,eff}} = D_{\text{A,K}}(\varepsilon/\xi) \). The following semi-empirical correlation, based on the kinetic theory of gases and proposed by Fuller et al. (1966), was used to calculate the ordinary binary diffusion coefficient for both anode and cathode: \( D_{\text{AB}} = 10\times10^{1.7\text{(1/2)} [(M_A + 1/M_B)^{0.5} P(v_A^{1/3} + v_B^{1/3})^2} \) (m\(^2\)/s) where subscripts \( A \) and \( B \) represent the gaseous components that make up the binary gas mixture (\( \text{H}_2\text{O} \) at the anode and \( \text{O}_2\text{N}_2 \) at the cathode). \( P \) is pressure in atmospheres and \( v_i \) is the Fuller diffusion volume, taken as 7.07, 12.7, 16.6 and 17.9 for \( \text{H}_2, \text{H}_2 \text{O}, \text{O}_2 \) and \( \text{N}_2 \) respectively (Fuller et al. 1966). Similar to the case of Knudsen diffusion, the effective ordinary diffusion coefficient is given by: \( D_{\text{AB,eff}} = D_{\text{AB}}(\varepsilon/\xi) \). The overall effective diffusion coefficient for each gas was then calculated using: \( 1/D_{\text{A,eff}} = 1/D_{\text{A,B,eff}} + 1/D_{\text{A,K,eff}}. \) Finally, the anode and cathode diffusion coefficients were calculated: \( D_{\text{tot,eff}} = (P_{\text{H}_2}P_{\text{SOFC}})D_{\text{H}_2\text{O,eff}} + (P_{\text{O}_2}P_{\text{SOFC}})D_{\text{H}_2\text{O,eff}} \) and \( D_{\text{tot,eff}} = D_{\text{O}_2\text{,eff}} \). \( \delta \) in Eq. (17) was found using: \( \delta = D_{\text{O}_2\text{,eff}}/(D_{\text{O}_2\text{,eff}} + D_{\text{H}_2\text{O,eff}}) \). The \( \gamma \) terms are the gas molar fractions in the bulk flow, taken as the average values of the anode and cathode inlet and outlet streams. This loss is low unless the current density is high and the fuel and air concentrations are low, caused by high utilisations \( (U_f \) and \( U_a \)). Under these conditions the limiting current may be reached reducing the fuel cell voltage to very low levels.

Finally, the actual voltage \( V \) was calculated using Eq. (18), which is simply the Nernst voltage less the sum of the voltage losses. The calculations described above are carried out using a design spec, which varies the input fuel flow until the SOFC stack DC power \( (P_{\text{el,DC}} = VI) \) equals a specified value (base case: 120 kW). However, for known current, as was the case for the current density sensitivity analysis (section 4.2.1.), a calculator block determines and sets the input fuel flow using: \( n\text{H}_2\text{,in} \) (kmol/h) = \( (I/2F)/(3600/1000) \) and \( n\text{Fuel}_{\text{in}} \) (kmol/h) = \( n\text{H}_2\text{,in} \times (\text{H}_2 + \text{yCO} + 4\text{CH}_4 + 7\text{yC}_2\text{H}_6 + 10\text{C}_3\text{H}_8 + 13\text{yC}_4\text{H}_{10}) \) where \( y \) is the molar fraction of gaseous component \( i \), then \( V \) and \( P_{\text{el,DC}} \) are calculated. In both cases, the gross and net AC efficiencies (LHV basis) are determined. The gross AC efficiency is defined as: \( \eta_{\text{G, gross}} = P_{\text{el,AC}}/(n\text{Fuel}_{\text{in}}\text{LHV}_{\text{fuel}}) \) where \( P_{\text{el,AC}} \) is the SOFC stack AC power (kW), \( n\text{Fuel}_{\text{in}} \) is the molar flow of input fuel (kmol/s) and \( \text{LHV}_{\text{fuel}} \) is the lower heating value of the input fuel (kJ/kmol). The net AC efficiency is defined as: \( \eta_{\text{G, net}} = (P_{\text{el,AC}} - P_{\text{comp}})/(n\text{Fuel}_{\text{in}}\text{LHV}_{\text{fuel}}) \) where \( P_{\text{comp}} \) is the electrical power requirement of the fuel and air compressors (kW).

4. RESULTS

4.1. Model validation

The developed model was validated against published data for the SPGI 100 kW CHP SOFC stack operating on natural gas. The model inputs were as follows (Campanari, 2001, Zhang et al. 2005):

- Natural gas composition (mole %): \( \text{CH}_4 81.3\% , \text{C}_2\text{H}_6 2.9\% , \text{C}_3\text{H}_8 0.4\% , \text{C}_4\text{H}_{10} 0.2\% , \text{N}_2 14.3\% , \text{CO}_2 0.9\% . \)
- Operating pressure \( (P_{\text{SOFC}}) \): 1.08 atm.
• Ejector pressure ratio ($P_{j,\text{in}}/P_{\text{SOFC}}$): 3.
• DC power ($P_{D,\text{DC}}$): 120 kW.
• Active area (S): 96.0768 m² (1152 cells).
• Operating / anode and cathode exhaust temperature ($T_{\text{op}}$): 910 °C.
• Input air / fuel temperature: 630 / 200 °C.
• $U_f / U_t / \text{STCR}$: 85% / 19% / 1.8.
• Cold and hot stream temperature difference (SOFC recuperator ‘HEATX1’): 10 °C.
• DC to AC inverter efficiency: 92%.

### Table 3. SOFC model validation

<table>
<thead>
<tr>
<th></th>
<th>Literature (Zhang et al. 2005)</th>
<th>Model results</th>
</tr>
</thead>
<tbody>
<tr>
<td>Voltage (V)</td>
<td>0.7</td>
<td>0.683</td>
</tr>
<tr>
<td>Current density (A/m²)</td>
<td>1780</td>
<td>1828.6</td>
</tr>
<tr>
<td>Air utilisation factor (%)</td>
<td>19</td>
<td>19</td>
</tr>
<tr>
<td>Pre-reforming temperature (°C)</td>
<td>536</td>
<td>535.1</td>
</tr>
<tr>
<td>Pre-reformer CH₄ conversion (%)</td>
<td>25.9</td>
<td>25</td>
</tr>
<tr>
<td>Pre-reformer higher hydrocarbon conversion (%)</td>
<td>100</td>
<td>100</td>
</tr>
<tr>
<td>Anode inlet gas composition (mole %)</td>
<td>H₂, 27, CO 5.6, CH₄ 10.1,</td>
<td>H₂, 26.9, CO 5.6, CH₄ 10.4,</td>
</tr>
<tr>
<td>Anode exhaust gas composition (mole %)</td>
<td>H₂, 27.9, CO 23.1, N₂ 6.2,</td>
<td>H₂, 27.8, CO 23.1, N₂ 6.2,</td>
</tr>
<tr>
<td>Cathode inlet temperature (°C)</td>
<td>821.32</td>
<td>823.7</td>
</tr>
<tr>
<td>Cathode exhaust gas composition (mole %)</td>
<td>O₂ 17.7, N₂ 82.3</td>
<td>O₂ 17.7, N₂ 82.3</td>
</tr>
<tr>
<td>Combustion products temperature (°C)</td>
<td>1012.35</td>
<td>1012.3</td>
</tr>
<tr>
<td>Stack exhaust temperature (°C)</td>
<td>833.85</td>
<td>833.7</td>
</tr>
<tr>
<td>Stack exhaust gas composition (mole %)</td>
<td>H₂O 4.5, CO 2.3, O₂ 15.9,</td>
<td>H₂O 4.5, CO 2.3, O₂ 15.9,</td>
</tr>
<tr>
<td>Gross AC efficiency (LHV) (%)</td>
<td>52</td>
<td>51.28</td>
</tr>
<tr>
<td>Net AC efficiency (LHV) (%)</td>
<td>-</td>
<td>49.15</td>
</tr>
</tbody>
</table>

The model results are in good agreement with published work (please refer to Tab. 3). There is only a slight difference for voltage, current density and efficiency. The reader should note that Zhang et al. (2005) used a very different method for calculating the voltage to the one applied in this work. They used semi-empirical correlations developed using a reference polarisation curve. For comparison, Campanari, (2001) reports a voltage and current density of 0.69 V and 1800 A/m² and a net AC efficiency of 48.5%. These results compare well with this work.

### 4.2. Sensitivity analyses

The model described was used to perform sensitivity analyses. The effects of varying $j$, STCR and $U_f$ on SOFC stack performance were investigated. During the sensitivity analyses the model input base case data was kept the same as for model validation with the following exceptions: fuel input (Glüssing biomass syn-gas) composition as given in section 2.1., input fuel temperature = 300 °C, $U_f = 16.7\%$ and STCR = 2.5.

Comparing SOFC stack operation on biomass gas to natural gas (see section 4.1.) at $j = 1828.6$ A/m², voltage was observed to decrease by 14 mV to 0.669 V, gross efficiency reduced 8.28% to 43%, net efficiency reduced 11.63% to 37.52% and DC power decreased 2.43 kW to 117.57 kW. The relatively large drop in efficiency is attributed to increased input fuel and air flow, which is due to the lower quality of the fuel gas. Even with this performance decrease the efficiency achieved is much higher than traditional biomass systems, making this technology very promising. For a required DC power of 120 kW using base case data and biomass syn-gas fuel the SOFC stack performance was as follows: $j = 1887$ A/m², $V = 0.662$ V, $\eta_{el,\text{gross}} = 42.53\%$ and $\eta_{el,\text{net}} = 37.04\%$. These have been identified as the optimum realistic operating conditions with regard to stack performance.

#### 4.2.1. Effect of current density

In this case the current was an input and the voltage and DC power were calculated. Figure 2 shows the effects of varying $j$ on the system. Increasing $j$ decreases both efficiency and voltage but increases power. Voltage is lowered as a result of higher voltage losses (ohmic, activation and concentration) and efficiency decreases due to increased input fuel flow. Increased $j$ requires the input air flow to increase to provide the O₂ ions for the electrochemical reaction, which in turn increases the air compressor parasitic power and lowers the efficiency. It is desirable with regard to operating costs, to operate the SOFC stack at a high voltage and efficiency; however it is also desirable with regard to capital costs, to operate the SOFC stack at high power (less SOFCs needed). Therefore there must be a trade-off between voltage, efficiency and power. A typical operating $j$ range is 1800 – 2000 A/m², corresponding to a cell voltage of 0.673 – 0.647 V. $\eta_{el,\text{gross}} = 43.2 – 41.6\%$, $\eta_{el,\text{net}} = 37.8 – 36.1\%$ and $P_{D,\text{DC}} = 116.36 – 124.41$ kW.
4.2.2. Effect of steam to carbon ratio

The effects of varying STCR are displayed in Fig. 3. STCR has a substantial impact on the pre-reformer, the inlet temperature increases from 408 to 729 °C over the STCR range, which in turn causes the anode temperature to rise (558 to 633 °C) and results in greater CH$_4$ conversion (0 to 92.2%). The high temperature and greater amount of steam available promotes the steam reforming of CH$_4$. The pre-reformer inlet temperature increases with STCR due to the recirculation of more high temperature depleted fuel, which is advantageous as the anode inlet gas will be closer to the SOFC operating temperature thus reducing the stack thermal gradient. On the other hand the greater flow into the pre-reformer means a larger pre-reformer is required and thus increased capital costs. Increasing STCR has a negative impact on voltage and efficiency and increases $j$, this is due to the change in anode temperature and gaseous component partial pressures, which decreases the Nernst voltage and increases the voltage losses. It is therefore desirable to operate the stack at low STCR. However the STCR must be high enough to ensure no carbon formation on the anode. Considering the findings above it is recommended to operate the SOFC stack at a STCR as low as possible but high enough as to ensure no carbon formation.

4.2.3. Effect of fuel utilisation factor

Figure 4 depicts the influence of $U_f$ on SOFC stack performance. The cell voltage decreases with $U_f$ as the fuel is more depleted, which increases the voltage losses. The current density increases due to the higher amount of H$_2$ consumed on the anode ($I = 2F_{\text{H}_2,\text{consumed}}$). The input fuel required to achieve the DC power of 120 kW decreases with $U_f$ because more of the energy contained in the fuel is converted to electricity and less to heat in the combustion plenum due to the higher H$_2$ consumed. Efficiency increases as a result of the reduced fuel input. The amount of recirculated fuel decreases with $U_f$ as less fuel needs to be recirculated to meet the specified STCR due to the increased H$_2$O content in the depleted fuel. As a result of less high temperature depleted fuel being recirculated the pre-reformer/anode temperature drops and thus the CH$_4$ conversion fraction is lowered. At low $U_f$ more of the fuel input is combusted, which results in a higher combustion temperature and therefore increased cathode and stack exhaust temperatures. As $U_f$ increases more of the fuel H$_2$ is converted to electricity meaning less is available to the combustion plenum thus lowering the combustion temperature and therefore the cathode and stack exhaust temperatures. Considering the findings above it is recommended to operate the SOFC stack at high fuel utilisation but below the level where the
concentration loss increases to a very high degree. A typical \( U_f \) is 0.85. However if the SOFC stack was thermally integrated with a gasifier then the level of heat available in the exhaust would need to be considered. In this case a low \( U_f \) would have to be used (typically 0.7) to ensure that sufficient heat was available to the gasifier.

![Figure 4](image)

**Figure 4.** Effect of fuel utilisation factor on (a) voltage, efficiency, input fuel flow and current density and (b) pre-reformer/anode temperature, cathode temperature, combustion temperature, stack exhaust temperature, recirculated fuel and methane conversion fraction

### 5. CONCLUSIONS

A computer simulation model of the SPGI 100 kW AC CHP tubular SOFC stack was developed using Aspen Plus. The objective of the work, which was to develop a computer simulation model flexible enough for use in industry and capable of predicting system performance under various operating conditions and using diverse fuels, was achieved. The objective was achieved by developing a model using existing Aspen Plus unit operation blocks with minimum requirements for linking of a subroutine thus reducing the model complexity and ensuring a short computational time. The model was validated against published data for the SPGI 100 kW SOFC stack operating on natural gas. Sensitivity analyses were carried out in order to give insight into the influence of the main variables on the system. The effects of varying current density \( j \), steam to carbon ratio \( STCR \) and fuel utilisation factor \( U_f \) on SOFC stack performance were investigated for the stack operating on biomass syn-gas (from Güssing DFB steam gasifier), the results of which revealed the following:

- There must be a trade-off between voltage, efficiency and power with respect to \( j \). For \( j = 1800 \) to 2000 A/m\(^2\), cell voltage = 0.673 to 0.647 V, DC power = 116.36 to 124.41 kW and electrical efficiency = 43.2 to 41.6\% (gross) and 37.8 to 36.1\% (net).
- The SOFC stack should be operated at a low \( STCR \) that is high enough to inhibit carbon formation.
- The SOFC stack should be operated at high \( U_f \) but below the level where the concentration loss increases to a very high degree.
- SOFC stack operation on biomass syn-gas compared to natural gas: voltage decreases by 14 mV to 0.669 V, gross efficiency reduced 8.28\% to 43\%, net efficiency reduced 11.63\% to 37.52\% and DC power decreased 2.43 kW to 117.57 kW. The drop in efficiency is attributed to increased input fuel and air flow due to the lower quality of the fuel gas. Even with this performance decrease the efficiency achieved is much higher than traditional biomass systems, making this technology very promising.
- The optimum realistic operating conditions with regard to stack performance were identified: \( STCR = 2.5, U_f = 0.85, DC \text{ power} = 120 \text{ kW}, j = 1887 \text{ A/m}^2, \text{cell voltage} = 0.662 \text{ V and electrical efficiency} = 42.53\% (\text{gross}) \) and 37.04\% (net).

Future work includes integration of the SOFC stack model with a biomass gasifier model where issues such as thermal integration and gas cleaning (tar elimination etc.) will be addressed.

### REFERENCES


Pröll, T., 2008, Private Communication, Vienna University of Technology, Vienna, Austria.


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