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A Framework for Generating Data to Simulate Application Scoring

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Abstract

In this paper we propose a framework to generate artificial data that can be used to simulate credit risk scenarios. Artificial data is useful in the credit scoring domain for two reasons. Firstly, the use of artificial data allows for the introduction and control of variability that can realistically be expected to occur, but has yet to materialise in practice. The ability to control parameters allows for a thorough exploration of the performance of classification models under different conditions. Secondly, due to non-disclosure agreements and commercial sensitivities, obtaining real credit scoring data is a problematic and time consuming task. By the provision of publicly available artificial data, credit scoring is opened to the wider data mining community. This in turn could help enable greater participation, promote replicable experimental findings, and give rise to solution proposals to outstanding credit scoring problems.

To ensure that our framework is sufficiently grounded in reality, data distributions are generated using a troika of sources: demographic information from the Central Statistics Office, Ireland; housing statistics published by the Irish Government Department of the Environment, Heritage and Local Government; and a profile of loan defaulters developed using a recent report published by a credit rating agency. By engaging with a credit scoring expert we select characteristics that are typical of most application scorecard models including, amongst others: age, income, loan value, and occupation. Through user controlled settings the conditional prior probabilities of the characteristics can be adjusted over time to simulate differing scenarios. In order to assign class labels to the generated data a credit risk score is estimated based on the non-linear interactions between various characteristics. Based on the desired number of defaulters a cut-off score is placed on this monotonic ordering of credit scores to distinguish between those likely to repay and those likely to default on their financial obligation. The classification complexity is controlled by adding user-defined random Gaussian noise.

After discussing the desirable characteristics of artificial data we describe a pseudo-random data generator for credit scoring and provide illustrations on how the framework can be used to generate population drift.

Keywords: Data Mining, Supervised Classification, Artificial Data, Simulation, Model Risk, Population Drift, Application Scoring

1. Introduction

The ongoing debt hangover affecting many private households (see Haldane, 2010) along with the fragile recovery in the financial system underlines the role of credit scoring in determining borrowers' access to credit. The term *credit scoring* is used to describe the process of evaluating the risk an applicant poses of defaulting on a financial obligation (Hand and Henley, 1997). The objective is to assign borrowers to one of two groups: *good* or *bad*. A member of the good group is considered likely to repay their financial obligation. A member of the bad group is considered likely to default on their financial obligation. The merits of credit scoring are well established in the literature and include reducing the cost of credit analysis, enabling faster credit decisions, closer monitoring of existing accounts, and prioritising collections (Brill, 1998). As credit scoring is essentially a discrimination problem

(good or bad), one may resort to the numerous classification techniques that have been suggested in the literature. Many of these classification models are derived from statistical methods, non-parametric methods, and artificial intelligence-based approaches (Lee *et al.*, 2005).

For an academic researcher, obtaining real credit scoring data with which to evaluate approaches is a problematic and time consuming task. This is due, in part, to commercial sensitivities and quite often acquiring real credit scoring data from a financial institution is simply an untenable task. It is therefore reasonable to regard the credit scoring research community, like many other research communities, as one that lacks a data sharing culture. This is not meant as a critique of the community itself but rather an acknowledgment of the barriers in sharing data.

In this paper we aim to address this issue by proposing a framework to generate artificial datasets that can be used in the design and assessment of classification techniques for credit scoring. This in turn could help enable: (i) greater participation and diversified perspectives; (ii) replicable experimental find-

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ings; (iii) increased creativity and solution proposals; and (iv) reduce time spent extracting, transforming and loading data.

To ensure that our framework is sufficiently grounded in reality, datasets are generated using a troika of sources: demographic information from the Central Statistics Office, Ireland (CSO, 2010); housing statistics published by the Irish Government Department of the Environment, Heritage and Local Government, or DEHLG, (DofE, 2008); and a profile of loan defaulters developed using market data from Moody’s Global Credit Research (Moody’s, 2010). By engaging with a credit scoring expert we select features that are typical of most application scorecard models including, amongst others, age; income; loan value; and occupation. In order to assign class labels to the generated data a credit risk score is estimated based on a set of non-linear, multi-feature rules designed in consultation with a credit scoring expert. Based on the desired default rate a cut-off score is placed on this monotonic ordering of credit scores to distinguish between those likely to repay and those likely to default on their financial obligation. The classification complexity is further controlled by adding random Gaussian noise with a mean of zero and a user adjustable standard deviation to this score.

The rest of the paper is organised as follows. In Section 2 we highlight how many of the datasets used in the literature are not publicly available, as well as the over-reliance on the few publicly available datasets. The advantages and motivations for using artificial data are discussed in Section 3. Section 4 presents our artificial data generation framework. The validity of our framework is assessed in Section 5. A demonstration of how the framework can be used to simulate population drift is provided in Section 6. Finally, future work and conclusions are presented in Section 7.

2. Background

In credit scoring, over the last decade numerous studies examining the performance of various models used to construct credit scorecards have been produced, (see West, 2000; Lee *et al.*, 2002; Baesens *et al.*, 2003; Hsieh, 2005; Ong *et al.*, 2005; Xiao *et al.*, 2006; Huang *et al.*, 2007a; Zhang *et al.*, 2007; Tsai and Wu, 2008; Nanni and Lumini, 2009; Zhou *et al.*, 2010; Khashman, 2010; Wang *et al.*, 2010; Kennedy *et al.*, 2010; Chen *et al.*, 2011). The popularity of such studies is motivated, in part, by the widely accepted view that the proposed or novel method can be accepted only if it is demonstrably superior to existing methods (Japkowicz and Shah, 2011). Many experts question the premise that a new methodology, using the same characteristics of the data as used by existing methods, produces a superior performance (see Hand, 2006b). A further concern is that the data used in these studies originates from two sources: (i) the Australian and German datasets which are publicly available from the University of California Irvine (UCI) Machine Learning Repository (Asuncion and Newman, 2007); and (ii) private datasets obtained from financial institutions.

The UCI repository serves several important functions (Salzberg, 1997). The repository allows published results to

be checked and through comparison with existing results researchers can assess the plausibility of a new algorithm. A number of researchers (Salzberg, 1997; Saitta and Neri, 1998; Soares, 2003; Martens *et al.*, 2011), however, caution against over-reliance on the UCI repository as a source of research problems. The repository is cited as a potential source of over-fitting. Researchers familiarity with datasets from the repository may influence them to design algorithms that are tuned to the datasets (Drummond, 2006). It is beneficial that researchers do not over-rely on the UCI repository, preferably multiple data sources should be used. For example, Keogh and Kasetty (2003) demonstrate how experimental results are greatly effected by the choice of test data and describe this phenomenon as *data bias* which is defined as “*the conscious or unconscious use of a particular set of testing data to confirm a desired finding.*” As a result researchers often ignore the problem of trying to understand under which conditions an algorithm works well or not (Soares, 2003).

Another issue with datasets from the UCI repository raised by researchers is that the datasets are not truly reflective of the real-world and only capture a small subset of all the situations that can arise in real-world situations (Saitta and Neri, 1998; Drummond and Holte, 2005; Drummond and Japkowicz, 2010). The Australian and German credit application datasets also contain very different class distributions and the overall size of the datasets is not representative of sizes that arise in practise. Such differences are likely to be an artefact of how the datasets were constructed, which in turn raises questions about how the data was collected (Drummond and Japkowicz, 2010). The inclusion of certain characteristics raises questions about the current relevancy of the UCI data. For example, in an age of the ubiquitous mobile phone, the use of a telephone characteristic in the German dataset is questionable. The assumption that the sample is random needs to be treated with caution and we should be careful not to derive too much from experimental results using such datasets (Drummond and Holte, 2005). As always it is desirable to use data derived from a richer source of diversity that captures a wider aspect of the world. Obtaining real-world data is a source of great frustration for those researchers who lack the necessary resources.

Fischer and Zigmond (2010) describe a number of factors impeding the sharing of data within academia, which are reiterated below.

Negative Career Impact. The need to publish is important to a researcher’s career and datasets used may be part of a long-term endeavour from which an individual could generate multiple publications. If a researcher is required to share data after their first publication the opportunity to generate further publications may be reduced if a better funded and resourced research group obtains the data. In fact, sharing data with others can be regarded as a means of providing them with a competitive advantage on publication by eliminating the need to collect and clean data. Another factor to consider is the lack of incentives to share data (Blumenthal *et al.*, 2006; Teeters *et al.*, 2008). Currently there are no metrics for sharing data which can be considered when awarding grants, promotions, or recog-

nition (citing the source of the dataset does alleviate this problem somewhat). Also, sharing data requires personnel to prepare the material for distribution. This in turn could result in reputational damage to the originator by a failure to have experimental results replicated based on poorly prepared data.

Limited Resources. Sharing data may require extra resources to convert it into an accessible form for other researchers. This reduces the time and money available to the originator to pursue their own research activities. Certain datasets may require updating and maintenance, once a researcher has completed their work it may be no longer feasible to store the data.

Property Rights and Legal Issues. As previously stated, legal and commercial reasons may prohibit the researcher from sharing data. Customer confidentiality, for example, is of the utmost importance for any financial institution. While with a single anonymised dataset it may not be possible to identify a particular individual, customer identity may be compromised through the combination of multiple datasets. A further restriction is that often data collected for one purpose may not be used for another purpose without requesting additional permission from the customers involved themselves.

Bergkamp (2002) believes that European Union data protection laws impose an onerous set of requirements on the data processor as data privacy is considered a “fundamental right” (EU, 1995). It is argued that restricting the flow of data between business and research, consumers ultimately receive outdated, lower quality products and services at higher prices (Bergkamp, 2002).

The authors are of the opinion that the above barriers will remain in place for the foreseeable future. Principally this is due to a lack of incentives, for the originator, to share data and the overly stringent requirements of data protection laws. Without the provision of publicly available datasets though, credit scoring will remain closed to the wider data mining community.

In domains where access to real-life data may simply be unattainable and to overcome the aforementioned limitations currently associated with machine learning data repositories, we contend that the use of artificial data is acceptable. It should be stressed that the data must be generated in the correct manner and be sufficiently grounded in reality in order to avoid the danger of investigating imaginary problems.

One may argue that as the UCI and other data repositories evolve over time, the quantity, quality, and variety of datasets will improve (Japkowicz and Shah, 2011). An advantage artificial data has over real-life data is the flexibility afforded to the manipulation of various parameters used in the evaluation process. This allows the researcher to design specific experiments aimed at evaluating algorithms’ performance under certain conditions of interest in a relatively precise manner (Scott and Wilkins, 1999; Japkowicz and Shah, 2011).

The practise of using research data generated by simulation is common in many other domains e.g. atmospheric and geophysical sciences (Reichle *et al.*, 2002), medicine (Robinson *et al.*, 2009), fraud detection (Lundin *et al.*, 2002), and intrusion detection (Lippmann *et al.*, 2000a,b). The next section examines

the applicability of artificial data to research problems, most notably in the credit scoring domain.

3. Artificial Data

Artificial data can be defined as “*data that are generated by simulated users in a simulated system, performing simulated actions*” (Lundin *et al.*, 2002). The terms *synthetic data*, *dummy data*, and *simulated data* are also used to describe artificial data.

In the following section we highlight previous work in artificial data generation along with its use in credit scoring. Following this we identify the characteristics of authentic data that should be present in artificial data.

3.1. Artificial Data: Previous Work

Researchers have often experimented with artificial data to test the efficacy of various classification algorithms across different data distributions. For example, Kim (2010) generated 324 simulated classification problems to evaluate the performance of the decision tree, neural network, and logistic regression techniques. Markham and Rakes (1998) used artificial data to compare linear regression and artificial neural network models across 20 datasets varying the sample size and the variance in the error. Scott and Wilkins (1999) describe two artificial data generators, one based on the multi-variate normal distribution and the other inspired by fractal techniques for synthesising artificial landscapes.

Often artificial data is used when only one class of data is available, i.e. fraud detection, intrusion detection, and fault detection. Fraud detection, areas of which involve the screening of credit applications and/or credit card transactions, is closely related to credit scoring. For similar legal and commercial reasons it is difficult to obtain authentic fraud datasets. Other than a relatively small automobile insurance dataset used by Phua *et al.* (2004) there are no publicly available datasets for studying fraud detection (Phua *et al.*, 2010). One approach used to address these data availability shortcomings is by using artificial data which closely matches authentic data. Barse *et al.* (2003) proposed a five-step artificial data generation methodology that can be used to generate new cases of fraud and variations of known frauds.

Intrusion detection is another domain where artificial data is also routinely used. DARPA (Lippmann *et al.*, 2000a,b) artificially generates network traffic and system call log files from a large computer network along with malicious software attacks. However, several contributions in the literature have highlighted concerns about the authenticity of the DARPA simulations (see McHugh, 2000; Mahoney and Chan, 2003). Other studies that have utilised artificial data to mimic network traffic and malicious intrusions in order to obtain a labelled training set include Debar *et al.* (1998); Theiler and Cai (2003); Hu and Panda (2004); Bertino *et al.* (2005); Steinwart *et al.* (2005); Abe *et al.* (2006). This list is by no means exhaustive but it serves to indicate the widespread use and acceptance of artificial data in the field of intrusion detection.

Fault detection is typically used to detect and identify faults in complex systems, e.g. flight control systems or environmental monitoring systems used in chemical processes. By monitoring all the information on a system it is possible to detect quantities that are over-sensitive to malfunctions (also referred to as residuals) (Heredia *et al.*, 2008). Due to safety, environmental and financial reasons artificial residual data is often used as an alternative means to introduce a fault into an expensive and complex system. In one such example Samy *et al.* (2011) use artificial data to simulate multiple sensor failure in an unmanned aircraft vehicle. Refer to Venkatasubramanian *et al.* (2003b,c,a) for a comprehensive overview of fault detection.

In credit scoring a straight-forward approach used to generate artificial data is to select data points from a multivariate distribution centred at alternate values and with various covariance matrices (see Hand and Adams, 2000; Fortowsky *et al.*, 2001). An even simpler approach is to use two univariate Gaussian distributions as this allows for visualisation of the model (see Kelly *et al.*, 1999; Hoffmann *et al.*, 2007). Publicly available artificial datasets such as Ripley's dataset (Ripley, 1994) have also been used (see Martens *et al.*, 2007). Hand (2004) observes that one of the limitations of artificial data is that it usually relates to problems which one would rarely encounter in practice e.g. intertwined spirals or chequerboard patterns. In addition, the previously listed examples of artificial data may miss the data structures typical of credit application data. It is important that generated artificial datasets should be based on reality. A number of participants at a workshop on evaluation methods for machine learning (Drummond *et al.*, 2006) espoused an artificial data generation framework which uses a real domain as input and by automated analyses of the input, variations of the dataset that follow some high level characteristics are generated. An example of such an approach is undertaken by Narasimhamurthy and Kuncheva (2007) who propose a framework for generating data to simulate changing environments through the introduction of deformations applied to the data. The deformations are brought about by simulating *population drift* - a term used to describe to changes in the probability distributions of the phenomena under study (Kelly *et al.*, 1999). However the generated data is either two dimensional or, importantly, requires an existing dataset from which to generate the data.

Many specialised dataset generators have been described in the literature. Examples include an IBM dataset generator (Almaden, 2004) which simulates a retail environment and produces market baskets of goods; and *celsim* (Myers, 1999) used in the genome assembly process by generating a user described DNA sequence with a variety of repeat structures along with polymorphic variants. Alaiz-Rodríguez and Japkowicz (2008) simulate a medical domain that states the prognosis of a patient a month after being diagnosed with influenza. Each patient is described using a number characteristics: (i) patient age; (ii) influenza severity; (iii) patient's general health; and (iv) patient's social status. Three of the characteristics (age, influenza severity, social status) are completely independent and one characteristic (general health) is dependent on two other characteristics (age, and social status). The prognosis class depends on

all four characteristics and the data is generated based on user defined prior probabilities for each characteristic. By manipulating the prior probabilities for each characteristic the user can simulate various scenarios (e.g. an increasingly virulent influenza outbreak, developing population, or poorer population). A number of general frameworks for generating data also exist (Atzmueller *et al.*, 2006; Melli, 2007), however such general frameworks cannot replicate the rich complexity and intricacies of a specific domain.

To the best of our knowledge no framework exists for generating artificial credit scoring data. The main purpose of our artificial data framework is to provide researchers with a means of creating artificial (but suitably realistic) credit scoring datasets with which to assess the behaviour of classification techniques which can, in turn, serve as an illustration used to help advance some research proposed direction in tool development, as per Liu *et al.* (2009). The use of artificial data to determine the superiority of some particular classification technique over another should be avoided. It is the opinion of the authors that the inherent unpredictability of real-world data cannot be replicated using artificial data. One cause of this unpredictability is the structural complexities arising from external and uncaptured circumstances (Scott and Wilkins, 1999). This cannot be replicated as structural regularity must be imposed on artificial data in the form of some fixed distributional model (Japkowicz and Shah, 2011). Furthermore, even though unintended, generated artificial data can be biased towards a particular classification technique that is capable of modelling the data more closely than others.

3.2. Properties of Data

As artificial data must be representative of authentic data it is necessary to define the required properties of authentic data. Within the literature, there are many properties that contribute towards data quality. Lindsay *et al.* (2010) conducted an analysis of the literature and found that the most common characteristics of data quality are accuracy, completeness, timeliness, relevance, understandability, accessibility and consistency. Data definition is an additional data quality characteristic identified by Baesens *et al.* (2009).

Data accuracy relates to the degree of precision of measurements of a feature to its true value (Baesens *et al.*, 2009). Listed among the typical causes of poor data accuracy include user input errors and errors in software. *Data completeness* refers to the extent to which values are missing in the data (Parker *et al.*, 2006). *Data relevance* corresponds as to whether the data addresses the users needs. For example, the selected sample should be as representative of the population for which the data mining model is intended. In credit scoring this is a difficult problem as populations change over time and a certain period of time must elapse before defaulters occur. This in turn requires us to consider *data timeliness*, which relates to the availability of the data in a user specified time frame. *Data understandability* addresses how easy it is to comprehend the data. Often, particularly in data mining, it is necessary to transform the data into a structure more amenable to data mining techniques. A popular example in credit scoring is to take the

logarithmic transformation of a continuous variable such as income which may then improve a data mining technique’s performance. *Data accessibility* refers to the ease with which the data can be retrieved when required (Lindsay *et al.*, 2010). *Data consistency* relates to situations in which multiple data sources are used and due to a lack of standardisation, two or more data items may conflict with each other. *Data definition* refers to the manner in which characteristics have been defined and how they impact the target variable (Baesens *et al.*, 2009). For example, it is standard practise to discretise a continuous variable (based on some measure such as the weights of evidence) to allow more stable correlation between variables and reduce the over reliance on certain characteristic values.

This section has examined previous work performed in generating artificial data. The limitations of artificial data, in terms of its usefulness in evaluating classification performance, were also highlighted. This section also identified the desired properties of real data, which artificial data should also contain.

4. Methodology

The following section explains the process of generating an artificial credit scoring dataset using our framework. The process is comprised of two stages: (i) Feature Generation; and (ii) Label Application, each of which will be explained in detail.

4.1. Feature Generation

Initially 15 separate characteristics are specified to describe the profile of a mortgage applicant. These characteristics are representative of the Irish mortgage market in 2007. The characteristics are selected based on two considerations: (i) the advice of an Irish credit risk expert; and (ii) the availability of official figures detailing the characteristics. Demographic information is obtained from the Central Statistics Office, Ireland (CSO, 2010). Housing statistics published by the Department of Environment, Heritage and Local Government, or DEHLG, (DofE, 2008) are also used to develop a borrower profile. For the class labelling process we utilise a recent Moody’s Global Credit Research report (Moody’s, 2010), which examined 17 portfolios of securities backed by Irish residential mortgages, profiling Irish loan defaulters. For explanation purposes we split the characteristics into two groups: borrower demographics and loan demographics. The borrower demographics are described in Table 1. Each of which is explained thereafter.

Table 1: Borrower demographics

Characteristic	Type	Description
First-Time-Buyer	Binary	Never purchased property
Age Group	Categorical	Age of the principal borrower
Income Group	Categorical	Combined income of the borrower(s)
Employment Sector	Categorical	Field of employment of primary borrower
Occupation	Categorical	Employment activity of primary borrower
Household Composition	Categorical	Family structure
Education	Categorical	Highest level of formal education
Expenses-to-Income	Continuous	Ratio of borrower expenditure to Income

First Time Buyer (FTB). This characteristic specifies whether or not the the borrower has previously purchased property. FTB is a binary flag, 1 (New Owner) or 0 (Previous Owner). Based on DEHLG statistics (DofE, 2008) (*Ownership status of borrowers* tab) the prior probabilities are conditional on Location and New Home as displayed in Table 2. Due to a lack of statistical information we do not differentiate between the prior probabilities of properties located outside of Dublin.

Table 2: List of conditional prior probabilities (CPP) for FTB characteristic

FTB	Location	New Home	CPP
1	Dublin	1	0.410
0	Dublin	1	0.590
1	Dublin	0	0.300
0	Dublin	0	0.700
1	Not Dublin	1	0.380
0	Not Dublin	1	0.620
1	Not Dublin	0	0.300
0	Not Dublin	0	0.700

Age Group. This characteristic specifies the age of the primary borrower. The 6 categories are defined based on categories previously employed by the DEHLG (DofE, 2008) (*Ranges of ages of borrowers* tab). The prior probabilities, displayed in Table 3, are conditional on the FTB characteristic.

Table 3: List of conditional prior probabilities (CPP) for Age characteristic

Age Category	FTB	CPP
18 - 25	1	0.180
26 - 30	1	0.400
31 - 35	1	0.230
36 - 40	1	0.100
41 - 45	1	0.050
46 - 55	1	0.040
18 - 25	0	0.040
26 - 30	0	0.160
31 - 35	0	0.230
36 - 40	0	0.200
41 - 45	0	0.150
46 - 55	0	0.220

Income Group. The combined annual income of the primary (and secondary) borrower is captured by this characteristic. Based on data contained in the DEHLG housing statistics (DofE, 2008) (*Range of income of borrowers* tab), 6 categories and prior probabilities (conditional on Location and FTB) are specified in Table 4. In order to validate the data with the Moody’s report (Moody’s, 2010) it was necessary to increase the parameter values of the Income Groups as follows: (i) 0 to 50,000 is now 40,000 to 60,000; (ii) 50,000 to 60,000 is now 60,000 to 80,000; (iii) 60,000 to 70,000 is now 80,000 to 100,000; (iv) 70,000 to 80,000 is now 100,000 to 120,000; (v)

Exceeding 80,000, which has been split into two categories, the first of which *120,000 to 150,000*; and (vi) *Exceeding 80,000*, the second of which, *150,000+*. As per Age Group, an actual income value for each borrower is a randomly generated value between the category parameter values. For the final income category a value is generated using a Pearson distribution with user defined skewness and kurtosis.

Table 4: List of conditional prior probabilities (CPP) for the Income Group categories (Income is listed in '000)

Category	Location	FTB	CPP
40 - 60	Dublin	1	0.066
60 - 80	Dublin	1	0.148
80 - 100	Dublin	1	0.199
100 - 120	Dublin	1	0.192
120 - 150	Dublin	1	0.200
150+	Dublin	1	0.195
40 - 60	Dublin	0	0.040
60 - 80	Dublin	0	0.062
80 - 100	Dublin	0	0.096
100 - 120	Dublin	0	0.111
120 - 150	Dublin	0	0.300
150+	Dublin	0	0.391
40 - 60	Not Dublin	1	0.173
60 - 80	Not Dublin	1	0.215
80 - 100	Not Dublin	1	0.213
100 - 120	Not Dublin	1	0.157
120 - 150	Not Dublin	1	0.120
150+	Not Dublin	1	0.122
40 - 60	Not Dublin	0	0.090
60 - 80	Not Dublin	0	0.111
80 - 100	Not Dublin	0	0.131
100 - 120	Not Dublin	0	0.129
120 - 150	Not Dublin	0	0.200
150+	Not Dublin	0	0.339

Employment Sector. This characteristic represents the employment activity of the primary borrower. The data is contained in CSO (2010) (2007 column, Table 2.3, pg. 29) whose categories are based on the EU NACE Revision 2 classification (Eurostat, 2008). Modifications have been made by reducing the number of categories to 14, as per Table 5. The prior probability of the characteristic is conditional on the Occupation characteristic.

Occupation. This characteristic attempts to measure the borrower's seniority within their Employment sector. Two sources are used: (i) the CSO Broad Occupational Groupings (CSO, 2010) (2007 column, Table 2.5, pg. 32); and (ii) DEHLG housing statistics (DofE, 2008) (*Occupation of borrowers* tab). A new group, Self-Employed, has also been added based on Moody's report (Moody's, 2010). Occupation is split into 6 categories: (i) Manager, Administrator, and Professional (henceforth MAP); (ii) Associate professional and technical, Clerical and secretarial, Personal and protective service, and Sales (henceforth Office); (iii) Craft and related (henceforth Trade);

(iv) Plant and machine operative (henceforth Manual Op); (v) Other manual operators (henceforth Farmer); and (vi) Self-Employed. The prior probabilities are conditional on Income Group, Location and FTB, as per Table 6.

Household Composition. The make-up of the borrower's household is defined by this characteristic. Household composition is a strong indicator of potential financial outgoings, e.g. childcare fees, university fees. Based on data from CSO (2010) (Table 7.5, pg. 118) the characteristic is split into the following categories: (i) 1 Adult, no child < 18; (ii) 1 Adult, 1+ child < 18; (iii) 2 Adults, no child < 18; (iv) 3+ adults, no child < 18; (v) 2 Adults, 1+ child < 18; and (vi) Other. The prior probabilities of the characteristic are conditional on Income Group and FTB, as per Table 7.

Education. The Education characteristic captures the highest level of formal education attained by the primary borrower. The characteristic is divided into 7 categories used by the Irish educational system: (i) Primary or below (PB); (ii) Lower secondary (LS); (iii) Higher secondary (HS); (iv) Post leaving certificate (PLC); (v) Third level non-honours degree (TLND); (vi) Third level honours degree or above (TLHD); and (vii) Other. The data is based on 2009 data obtained from CSO (2010) (Table 2.4, pg. 31). The prior probabilities of the characteristic are conditional on Income Group.

Expenses-to-Income. This characteristic represents the standard level of borrower expenditure on commodities and services. The data is derived from the most recent Household Budget Survey (CSO, 2010) conducted by the Central Statistics Office, Ireland. The survey is based on a representative random sample of all private households in the State, thus the results do not distinguish between those households that have recently entered the housing market and those that have been in the market for some considerable time. The following commodity groups are covered by the survey: Services and other expenses; Transport; Miscellaneous goods; Household durable goods; Household non-durable goods; Housing; Fuel and light; Clothing and footwear; Drink and tobacco; and Food. For the Housing group the mortgage repayments and rent charges have been removed. This is performed as an attempt to minimise the differences between those households that have recently entered the housing market and those that have been in the market for a considerable time.

Each primary borrower is assigned a value representative of the percentage of income spent on household expenses, an Expenses-to-Income ratio. The prior probabilities of the Expenses-to-Income ratio are conditional on Income Group (Table 9) and Household Composition (Table 10). This results in two Expenses-to-Income ratios being generated for each borrower: (i) Expenses-to-Income based on Income Group; and (ii) Expenses-to-Income based on Household Composition. When calculating (i) and (ii) for each borrower, a small user-defined random variance taken from a normal distribution is added (subtracted) to (from) each ratio. The average of (i) and (ii) is then calculated for each borrower resulting in a final Expenses-to-Income value.

Table 5: List of conditional prior probabilities (CPP) for Employment Sector categories, which are conditional on the categories of the Occupation characteristic

Category	CPP of MAP	CPP of Office	CPP of Trade	CPP of Manual Op.	CPP of Farmer	CPP of Self-Employed
Agriculture, Forestry and fishing	0.01	0.01	0.05	0.05	0.75	0.05
Construction	0.01	0.02	0.30	0.40	0.00	0.13
Wholesale, Retail	0.12	0.25	0.10	0.03	0.03	0.14
Transportation, Storage	0.03	0.02	0.03	0.10	0.03	0.04
Hospitality	0.11	0.06	0.05	0.05	0.00	0.06
Information, Communication	0.08	0.08	0.00	0.00	0.00	0.03
Professional, Scientific, Technical	0.15	0.07	0.00	0.00	0.00	0.05
Admin., Support services	0.06	0.07	0.03	0.00	0.00	0.04
Public Admin.	0.05	0.05	0.05	0.05	0.05	0.05
Education	0.12	0.10	0.00	0.00	0.00	0.07
Health	0.13	0.10	0.05	0.03	0.00	0.10
Industry	0.02	0.01	0.30	0.25	0.10	0.14
Financial	0.09	0.12	0.00	0.00	0.00	0.05
Other	0.04	0.04	0.04	0.04	0.04	0.05

Table 6: List of conditional prior probabilities (CPP) for the Occupation categories. The CPP are derived from the Income Group categories (displayed in '000), and Location.

Category	Location	FTB	CPP of Income 40 - 60	CPP of Income 60 - 80	CPP of Income 80 - 100	CPP of Income 100 - 120	CPP of Income 120 - 150	CPP of Income 150+
MAP	Dublin	1	0.08	0.13	0.13	0.35	0.40	0.48
Office	Dublin	1	0.34	0.41	0.42	0.42	0.42	0.39
Trade	Dublin	1	0.35	0.28	0.27	0.10	0.07	0.03
Manual Op.	Dublin	1	0.12	0.07	0.07	0.03	0.01	0.00
Farmer	Dublin	1	0.01	0.01	0.01	0.00	0.00	0.00
Self-Employed	Dublin	1	0.10	0.10	0.10	0.10	0.10	0.10
MAP	Dublin	0	0.12	0.26	0.33	0.51	0.66	0.78
Office	Dublin	0	0.48	0.48	0.45	0.32	0.22	0.11
Trade	Dublin	0	0.22	0.12	0.09	0.07	0.02	0.01
Manual Op.	Dublin	0	0.08	0.04	0.03	0.00	0.00	0.00
Farmer	Dublin	0	0.00	0.00	0.00	0.00	0.00	0.00
Self-Employed	Dublin	0	0.10	0.10	0.10	0.10	0.10	0.10
MAP	Not Dublin	1	0.03	0.05	0.09	0.14	0.18	0.20
Office	Not Dublin	1	0.17	0.15	0.16	0.26	0.39	0.40
Trade	Not Dublin	1	0.40	0.35	0.35	0.30	0.25	0.25
Manual Op.	Not Dublin	1	0.20	0.25	0.20	0.10	0.03	0.00
Farmer	Not Dublin	1	0.10	0.10	0.10	0.10	0.05	0.05
Self-Employed	Not Dublin	1	0.10	0.10	0.10	0.10	0.10	0.10
MAP	Not Dublin	0	0.10	0.24	0.33	0.50	0.63	0.73
Office	Not Dublin	0	0.42	0.35	0.32	0.24	0.18	0.09
Trade	Not Dublin	0	0.28	0.22	0.16	0.09	0.04	0.03
Manual Op.	Not Dublin	0	0.07	0.06	0.06	0.04	0.00	0.00
Farmer	Not Dublin	0	0.03	0.03	0.03	0.03	0.05	0.05
Self-Employed	Not Dublin	0	0.10	0.10	0.10	0.10	0.10	0.10

Table 7: List of conditional prior probabilities (CPP) for the Household Composition categories. The CPP are derived from the Income Group categories (displayed in '000), and FTB.

Category	FTB	CPP of Income 40 - 60	CPP of Income 60 - 80	CPP of Income 80 - 100	CPP of Income 100 - 120	CPP of Income 120 - 150	CPP of Income 150+
1 Adult, no child < 18	1	0.300	0.300	0.250	0.200	0.220	0.180
1 Adult, 1+ child < 18	1	0.330	0.200	0.100	0.050	0.010	0.020
2 Adults, No child	1	0.130	0.170	0.220	0.300	0.380	0.330
3 Adults, No child < 18	1	0.020	0.060	0.080	0.080	0.020	0.030
2 Adults, 1+ child < 18	1	0.120	0.170	0.250	0.270	0.270	0.340
Other	1	0.100	0.100	0.100	0.100	0.100	0.100
1 Adult, no child < 18	0	0.250	0.270	0.170	0.120	0.100	0.100
1 Adult, 1+ Children < 18	0	0.230	0.100	0.070	0.050	0.010	0.020
2 Adults, No child	0	0.150	0.170	0.250	0.270	0.300	0.300
3 Adults, No child < 18	0	0.020	0.060	0.080	0.080	0.030	0.030
2 Adults, 1+ Child < 18	0	0.250	0.300	0.330	0.380	0.460	0.450
Other	0	0.100	0.100	0.100	0.100	0.100	0.100

Table 8: List of conditional prior probabilities (CPP) for the Education categories. The CPP are derived from the Income Group categories (displayed in 000).

Category	CPP of Income 40 - 60	CPP of Income 60 - 80	CPP of Income 80 - 100	CPP of Income 100 - 120	CPP of Income 120 - 150	CPP of Income 150+
PB	0.200	0.050	0.010	0.010	0.000	0.000
LS	0.200	0.100	0.020	0.010	0.010	0.000
HS	0.250	0.150	0.040	0.020	0.010	0.010
PLC	0.150	0.250	0.180	0.100	0.050	0.030
TLND	0.100	0.280	0.340	0.280	0.300	0.300
TLHD	0.070	0.140	0.380	0.550	0.600	0.630
Other	0.030	0.030	0.030	0.030	0.030	0.030

Table 9: Expenses-to-Income ratios conditional on Income Group category (displayed in '000). For each Income Group category a Variance range, from which a value is randomly selected to be added (subtracted) to (from) Expenses-to-Income, is displayed.

Income Group	Expenses-to-Income	+/- Variance Range
40 - 60	0.541	0.050
60 - 80	0.514	0.050
80 - 100	0.477	0.050
100 - 120	0.418	0.060
120 - 150	0.380	0.075
150+	0.313	0.100

Table 10: Expenses-to-Income ratios conditional on Household Composition category (displayed in '000). For each Household Composition category a Variance range, from which a value is randomly selected to be added (subtracted) to (from) Expenses-to-Income, is displayed.

Household Composition	Expenses-to-Income	+/- Variance Range
1 Adult, no child < 18	0.401	0.050
2 Adults, No child	0.384	0.100
1 Adult, 1+ Children < 18	0.489	0.050
2 Adults, 1+ Child < 18	0.380	0.100
3 Adults, No child < 18	0.370	0.050
Other	0.451	0.050

The loan profile demographics are described in Table 11. Each of the characteristics are explained below.

Table 11: Loan demographics

Characteristic	Type	Description
Location	Categorical	Location of purchased dwelling
New Home	Binary	Newly built dwelling
Loan Value	Categorical	Amount advanced to the borrower
LTV	Categorical	Loan-to-value ratio
Loan Term	Categorical	Length of the loan in years
Loan Rate	Categorical	Interest rate paid on the loan
House Value	Categorical	Market value of the property
MRTI	Continuous	Ratio of mortgage-repayments-to-income

Location. This characteristic provides a breakdown of the loans in terms of the regional concentration. The categories and respective figures were obtained from a Fitch Ratings analysis on an AIB portfolio of over 65,000 mortgages (Fitch Ratings, 2007). Table 12 lists the 6 categories along with the initial prior probabilities.

New Home. This characteristic specifies if the borrower is purchasing a newly built property or a previously occupied property. The prior probabilities are displayed in Table 13. The data is obtained from DEHLG housing statistics (DofE, 2008) (*Ownership status of borrowers* tab). The characteristic is not actually used during the labelling process (see Section 4.2). It is only used in the data generation process as part of the statis-

Table 12: List of prior probabilities for Location characteristic

Location	Prior Probability
Dublin	0.32
Cork	0.15
Galway	0.07
Limerick	0.04
Waterford	0.03
Other	0.39

tics provided by the DEHLG (DofE, 2008) are based on this characteristic.

Table 13: List of prior probabilities for New Home characteristic

Location	Prior Probability
New Home	0.46
Old Home	0.54

Loan Value Group. This characteristic describes the principal of the loan. The nine categories and prior probabilities used by Loan Value Group are similar to those used by DEHLG housing statistics (DofE, 2008) (*Range of loans paid* tab), the difference being we further sub-divided the final two categories resulting in two additional categories. The prior probabilities, conditional on the Location; New Home; and FTB characteristics, are specified in Table 14. The precise loan value for each borrower is a randomly generated value between the category start and end values. For simplicity we restrict the maximum loan value to 900,000. We employ the assumption that any values greater than this amount require an additional assessment of creditworthiness in the form of a personal interview with a member of the bank's staff.

Loan-to-Value (LTV). This characteristic expresses the ratio of the loan value to the market value of the asset. Based on data from DEHLG housing statistics (DofE, 2008) (*Ranges of loans to value* tab) we use 10 categories ranging from 45% to 100%, as per Table 15. We subdivide one of the original categories ("Up to 70%") into five separate categories as its conditional prior probability was quite large (52% in some cases). The prior probabilities of the LTV categories are conditional on the Location, New Home, and FTB characteristics.

Loan Term. The duration of the loan in years is captured by the Loan Term characteristic. The data is based on DEHLG housing statistics (DofE, 2008) (*Ranges of loan terms* tab). Five categories are employed: (i) 20 years; (ii) 25 years; (iii) 30 years; (iv) 35 years; and (v) 40 years. The prior probabilities are conditional on Location and FTB. We have also added Age Group as a conditional prior probability to ensure the values are realistic, as per Table 16.

House Value. This characteristic represents the market value of the asset. It is calculated as Loan Value divided by Loan-To-Value. House Value is generated as a continuous value that is then converted in a categorical value. The categorical values are based on categories used by DEHLG housing statistics (DofE, 2008) (*Range of house prices* tab), with one of the categories (300,001 to 400,000) subdivided into two separate categories (300,001 to 350,000 and 350,001 to 400,000). The categories used are (i) 0 to 150,000; (ii) 150,001 to 200,000; (iii) 200,001 to 250,000; (iv) 250,001 to 300,000; (v) 300,001 to 350,000; (vi) 350,001 to 400,000; (vii) 400,001 to 500,000; (viii) 500,001+.

Loan Rate. This characteristic represents the interest rate paid by the borrower on the loan. For the simplicity of the monthly mortgage repayments we do not consider interest only loans. The breakdown between Fixed and Variable interest rate loans is provided by DEHLG housing statistics (DofE, 2008) (*Fixed & var interest rate loans* tab). We further subdivide these two categories into 6 categories: (i) Fixed - Over 5 years; (ii) Tracker Type 1; (iii) Tracker Type 2; (iv) Standard Variable; (v) Up to 1 year fixed; and (vi) Fixed - 3 to 5 years, as per Table 17

Table 17: Loan Rate prior probabilities

Loan Rate Description	Interest Rate	Prior Probability
Fixed - Over 5 years	0.0535	0.450
Tracker Type 1	0.0150	0.150
Tracker Type 2	0.0250	0.100
Standard Variable	0.0350	0.150
Up to 1 year fixed	0.0450	0.090
Fixed - 3 to 5 years	0.0500	0.060

Monthly-Repayments-to-Income (MRTI). This is a continuous characteristic which expresses monthly mortgage repayments as a percentage of monthly income.

All of the above conditional prior probabilities are user defined parameters, the values we have specified attempt to replicate the Irish mortgage market in 2007. Another user defined parameter is the population size of the data to be generated, the default value is 2,000 instances.

4.2. Label Application

For each instance generated, the constituent characteristics are assigned a risk score which are then aggregated into an overall risk score for the instance. The higher the risk score, the greater the likelihood of default. Coded business intelligence rules are used to determine the risk score of a characteristic value. These business intelligence rules have been devised as a product of extensive consultations with a credit risk scorecard expert. Additional information was also provided in the Moody's report (Moody's, 2010) on Irish defaulters and a Central Bank of Ireland technical report (McCarthy and McQuinn, 2010). By presenting a realistic assessment of credit

Table 14: Loan Value Group conditional prior probabilities (LVGCCP) for each Loan Value Group category. Loan Value Group values are displayed in '000. The CPP of each row should sum to 1. Certain locations have been combined, Wtf = Waterford.

Location	FTB	New Home	LVGCCP 50 - 100	LVGCCP 100 - 150	LVGCCP 150 - 200	LVGCCP 200 - 250	LVGCCP 250 - 300	LVGCCP 300 - 350	LVGCCP 350 - 400	LVGCCP 400 - 450	LVGCCP 450 - 900
Dublin	1	1	0.01	0.03	0.13	0.30	0.27	0.12	0.07	0.06	0.01
Dublin	0	1	0.02	0.04	0.10	0.15	0.18	0.13	0.14	0.16	0.08
Dublin	1	0	0.01	0.03	0.06	0.13	0.25	0.28	0.10	0.11	0.03
Dublin	0	0	0.08	0.05	0.08	0.12	0.15	0.13	0.12	0.15	0.12
Cork \Galway	1	1	0.06	0.14	0.31	0.24	0.17	0.07	0.01	0.01	0.00
Cork \Galway	0	1	0.08	0.13	0.21	0.22	0.15	0.11	0.04	0.05	0.02
Cork \Galway	1	0	0.04	0.08	0.18	0.27	0.23	0.12	0.05	0.02	0.00
Cork \Galway	0	0	0.11	0.13	0.19	0.17	0.11	0.16	0.09	0.02	0.02
Limerick \Wtf	1	1	0.06	0.16	0.34	0.25	0.13	0.05	0.01	0.01	0.00
Limerick \Wtf	0	1	0.10	0.18	0.23	0.23	0.15	0.05	0.04	0.02	0.01
Limerick \Wtf	1	0	0.06	0.12	0.20	0.25	0.22	0.11	0.02	0.01	0.01
Limerick \Wtf	0	0	0.23	0.19	0.22	0.18	0.11	0.02	0.02	0.02	0.02
Other	1	1	0.05	0.15	0.36	0.28	0.11	0.04	0.01	0.01	0.00
Other	0	1	0.10	0.11	0.24	0.17	0.18	0.08	0.05	0.05	0.03
Other	1	0	0.05	0.14	0.24	0.28	0.18	0.08	0.02	0.01	0.01
Other	0	0	0.16	0.20	0.21	0.17	0.14	0.04	0.03	0.03	0.02

Table 15: LTV conditional prior probabilities (LTVCPP) for each LTV category. The CPP of each row should sum to 1.

Location	New Home	FTB	LTVCPP 0.45	LTVCPP 0.55	LTVCPP 0.6	LTVCPP 0.65	LTVCPP 0.7	LTVCPP 0.75	LTVCPP 0.85	LTVCPP 0.93	LTVCPP 0.975	LTVCPP 1
Dublin	1	1	0.010	0.020	0.020	0.030	0.040	0.080	0.130	0.270	0.200	0.200
Dublin	0	1	0.010	0.020	0.020	0.030	0.040	0.070	0.160	0.430	0.050	0.170
Dublin	1	0	0.020	0.030	0.040	0.110	0.150	0.170	0.230	0.180	0.020	0.050
Dublin	0	0	0.030	0.030	0.100	0.120	0.130	0.150	0.180	0.190	0.020	0.050
Not Dublin	1	1	0.030	0.030	0.030	0.040	0.110	0.080	0.110	0.200	0.090	0.280
Not Dublin	0	1	0.010	0.010	0.020	0.030	0.040	0.070	0.160	0.420	0.040	0.200
Not Dublin	1	0	0.040	0.080	0.120	0.100	0.120	0.150	0.160	0.130	0.010	0.090
Not Dublin	0	0	0.030	0.060	0.090	0.160	0.150	0.140	0.170	0.140	0.010	0.050

Table 16: Loan Term conditional prior probabilities (LTCPP) for each Loan Term category. The CPP of each row should add to 1.

Location	FTB	Age	LTCPP 20	LTCPP 25	LTCPP 30	LTCPP 35	LTCPP 40
Dublin	1	18 - 25	0.010	0.030	0.080	0.800	0.080
Dublin	1	26 - 30	0.020	0.060	0.160	0.720	0.040
Dublin	1	31 - 35	0.020	0.060	0.160	0.720	0.040
Dublin	1	36 - 40	0.020	0.060	0.160	0.720	0.040
Dublin	1	41 - 45	0.100	0.730	0.120	0.050	0.000
Dublin	1	46 - 55	0.120	0.750	0.080	0.050	0.000
Dublin	0	18 - 25	0.120	0.140	0.210	0.480	0.050
Dublin	0	26 - 30	0.230	0.280	0.220	0.240	0.030
Dublin	0	31 - 35	0.220	0.320	0.190	0.240	0.030
Dublin	0	36 - 40	0.220	0.320	0.190	0.240	0.030
Dublin	0	41 - 45	0.220	0.320	0.250	0.200	0.010
Dublin	0	46 - 55	0.220	0.320	0.240	0.220	0.000
Not Dublin	1	18 - 25	0.030	0.050	0.170	0.680	0.070
Not Dublin	1	26 - 30	0.050	0.090	0.180	0.620	0.060
Not Dublin	1	31 - 35	0.060	0.110	0.200	0.590	0.040
Not Dublin	1	36 - 40	0.060	0.110	0.200	0.590	0.040
Not Dublin	1	41 - 45	0.140	0.290	0.300	0.250	0.020
Not Dublin	1	46 - 55	0.340	0.390	0.140	0.130	0.000
Not Dublin	0	18 - 25	0.060	0.090	0.120	0.410	0.320
Not Dublin	0	26 - 30	0.140	0.150	0.250	0.320	0.140
Not Dublin	0	31 - 35	0.220	0.330	0.240	0.190	0.020
Not Dublin	0	36 - 40	0.220	0.330	0.240	0.190	0.020
Not Dublin	0	41 - 45	0.130	0.460	0.290	0.100	0.020
Not Dublin	0	46 - 55	0.140	0.680	0.100	0.080	0.000

risk, the business intelligence rules generate non-linear distributions based on interactions between the characteristics. Interactions occur when different predictive patterns exist for different subgroups within the population (Anderson, 2007). Without any such attempt to define the interactions between the characteristics, the generated dataset would otherwise present a trivial classification task. The rest of this section outlines the business intelligence rules and specified interactions used to generate labels. The characteristics with which a specific characteristic has an interaction are listed in parentheses. Figure 1 also illustrates the interactions between the characteristics. After the credit risk score of an instance is calculated a user defined noise random Gaussian noise can be added (subtracted) to (from) this value. Based on a user specified bad rate, a cut-off score is identified whereby those instances with a value equal to or greater than the cut-off score are labelled as defaulters (Bads) and those less than the cut-off score are labelled as repayers (Goods). In order to complicate the classification task and to mimic real-world unpredictability, a user-defined swap rate can then be applied, whereby a percentage of repayers are randomly selected and their labels are reassigned as defaulter.

MRTI (Loan Rate, Expenses-to-Income). In general, when granting credit, a safe figure for a borrower's MRTI should be no more than 33%. The Loan Rate is one of the main variables used when calculating the monthly mortgage repayment amount. The Expenses-to-Income ratio and MRTI should both be able to provide a clear indication of a borrower's overall expenditure. A borrower with a relatively high MRTI (33% - 38%) may initially appear a risky prospect. However, this risk is reduced somewhat if their Expenses-to-Income ratio is low and their Loan Rate is fixed (i.e. the loan repayments are not subject to any variability for the foreseeable future). For scoring purposes the MRTI is split into 5 equal sized monotonically-ordered quantiles. However, the size of the quantiles may differ after unrealistic values have been removed. After the labelling process has been completed the MRTI ratios are stored as continuous values.

Loan Value Group (Income Group, LTV). The business intelligence rules are coded under the assumption that the higher the loan value the greater the risk of default, as per Moody's report (Moody's, 2010). However, this risk may be offset by a high level of Income or a low LTV. A high level of income indicates the borrower's ability to service a large loan. A low LTV suggests that the borrower has already invested too much in the loan to simply walk away.

Employment Sector (Location, Education). The Employment Sector represents, to some degree, the borrower's job security and earnings. For example, a borrower employed by the government is considered less risky than a construction worker. Location is included as it relates to the availability of commensurate employment opportunities within the same locale, i.e. the size of the jobs market. For example, a borrower working in the Industry sector in a sparsely populated area, such as Waterford, is considered a risk as there are fewer opportunities to

find alternative employment in the same Industry as compared to a larger and more industrially active centre such as Dublin. Education attempts to capture the skill set of the borrower. The business intelligence rules operate under the assumption that the more educated the borrower, the easier to move between employment sectors.

Occupation (Employment Sector, Expenses-to-Income). Based on (Moody's, 2010) we assign self-employed borrowers as the most likely to default. Borrowers belonging to the Manager, Administrator, and Professional (MAP) Employment Sector category are considered the least likely to default - due to their importance to an organisation as well as the demand for their skills and experience. The Employment Sector characteristic helps determine the demand for a particular Occupation. For example, a bureaucratic sector such as Health would have a higher demand for MAP employees than a sector such as Hospitality. By using a borrower's Occupation along with their Expenses-To-Income the business intelligence rules attempt to capture the borrower's social status and the cost to maintain it.

Location (House Value Group, Occupation). The ability to sell or rent a house can reduce the likelihood of default. Dublin and Cork are the main rental markets in Ireland and as such represent a lower risk of default. For the next three locations: Galway, Limerick, and Waterford the risk of default increases proportionally as the size of the rental market decreases. Other is considered the riskiest location of the six as it represents the least densely populated areas. House Value is used to indicate that for some locations (i.e. Dublin) houses are over valued, as per 2007. The more overpriced a home, the greater the risk of default on account of the negative equity that may arise when house prices return to their longterm average. Occupation, in the context of Location, indicates that the level of demand for a borrower's expertise and experience varies from location to location. Typically, a populous location indicates a large and diverse jobs market.

Income Group (Household Composition, MRTI). A borrower with a high level of income is considered less likely to default. Household Composition is used to indicate the level of income required to maintain the household. Ordinarily, 2 Adults, 1+ child < 18 is considered to have a lower chance of default compared to 2 Adults, No child as they are more likely to have stronger community ties through family involvement. The MRTI indicates the amount of income required to service the loan. For example, a borrower on a high income with a high MRTI is considered a greater default risk than a borrower on a mid-level income with a low MRTI.

Household Composition (Age Group, MRTI). The Household Composition affects the risk of default with regard to earnings power, and the priorities of household members. A single person household represents a higher risk of defaulting compared to the 2 Adults, No child category as the impact of a loss of income to the couple may be less severe. From a Household Composition perspective, the Age Group represents the type of

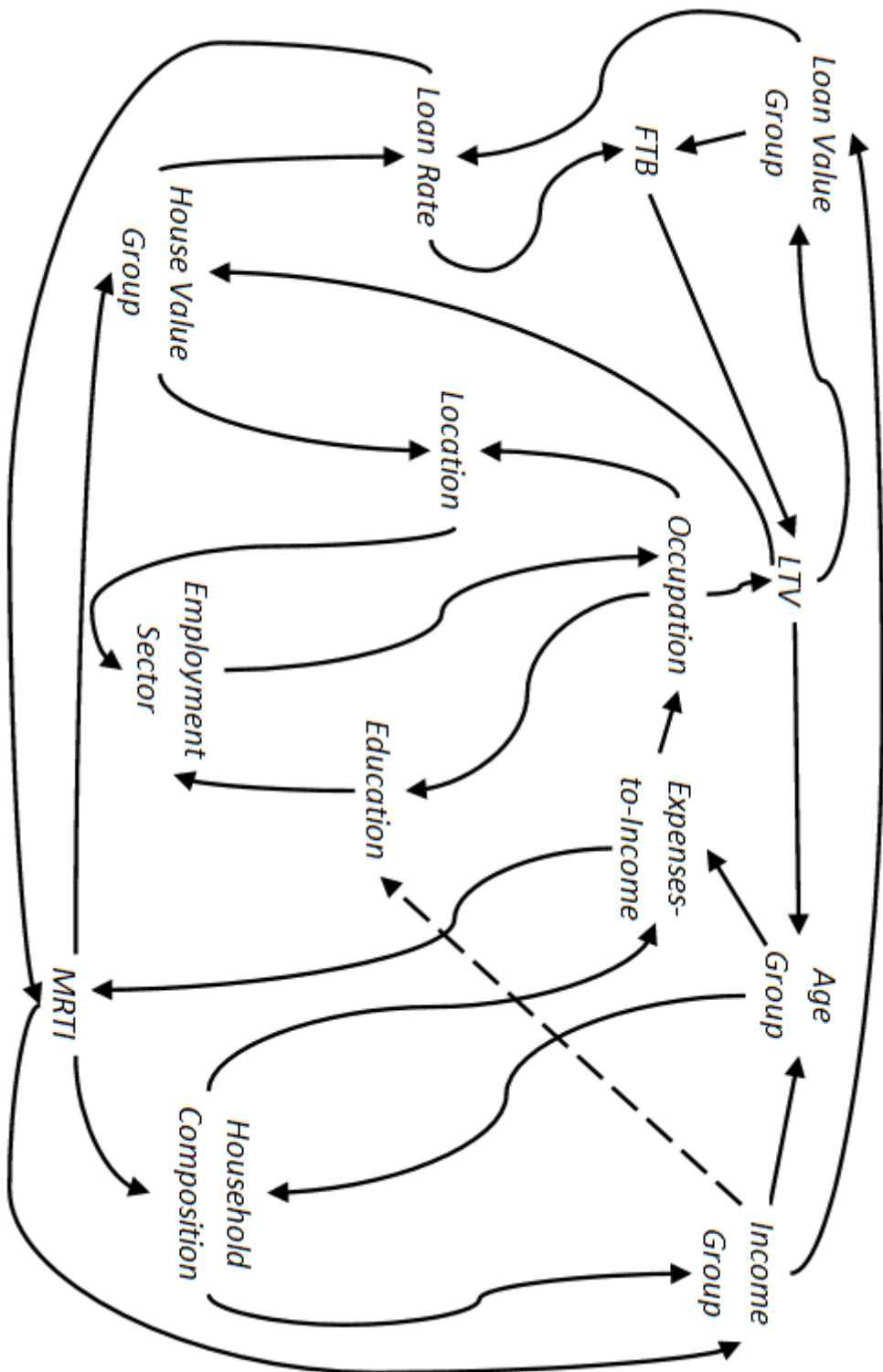


Figure 1: Interactions between the dataset characteristics

dependencies the borrower may have. For example a young 2 Adults, 1+ child < 18 will likely have to pay for school/doctor fees. The MRTI indicates the burden the household is under to pay bills. A household with no dependents and a high MRTI is less risky than a household with children and a high MRTI, as the welfare of the children will come first.

Age Group (Income Group, LTV). Younger borrowers represent a greater risk of default than older borrowers. However, older borrowers still present a risk due to illness and death. Income Group, in the context of Age Group, indicates the present and future earning potential of a borrower. A young person on a high income can be interpreted as a skilled individual and therefore low risk. As the LTV reflects the amount of savings a borrower has contributed to the loan, the Age Group indicates how long the borrower has to rebuild their savings.

FTB (Loan Value Group, Loan Rate). Due to a lack of experience, a First-Time-Buyer is considered more likely to default on a loan than a non-FTB. A high Loan Value Group places greater pressure on the borrower to manage their finances. The Loan Rate indicates the borrower's financial aptitude at selecting an appropriate loan product. For example a FTB with a fixed rate is considered risk averse compared to a FTB with a variable rate.

Education (Income Group, Occupation). A borrower's level of formal Education impacts the risk of default. The more educated an individual, the more financially astute they are likely to be. A high level of education also improves job prospects. Income Group affects Education in terms of the ability to afford training courses and improve skill levels. A borrower's Occupation indicates their ability to apply their education in terms of over-achievement or under-achievement, i.e. a measure of their drive to overcome obstacles.

Loan Rate (House Value Group, Loan Value Group). There are three different Loan Rates: (i) Fixed rate loans which are considered the least risky; (ii) Tracker rate loans which are slightly more risky; and (iii) Variable rate loans which are considered the riskiest of the three. In terms of the Loan Rate, the Loan Value Group affects risk based on the fact that the size of the repayments increase with the size of the Loan Value. In general, interest rates can affect the availability of capital and demand for investment. As interest rates were at a historically low level in 2007, the business intelligence rules are based on the assumption that interest rates will rise. As interest rates rise, a more expensive house will be harder to sell. Rising interest rates may cause the house value to decline, and increase the possibility of negative equity.

Expenses-To-Income (Household Composition, Age Group). The greater the Expenses-to-Income ratio the higher the risk of default. Household Composition is a strong indicator of how much money the borrower needs to spend on groceries, utility bills, fees etc. The Age group helps identify the level and the necessity of the expenses. For example, a young single person would be expected to have a high Expenses-to-Income ratio but

much of it may involve expenditure on items such as holidays or concert tickets. During the labelling process the Expenses-to-Income ratios are split into 5 equal sized monotonically-ordered quantiles. However, the size of the quantiles may differ after unrealistic values have been removed. After the labelling process has been completed the Expenses-to-Income ratios are stored as continuous values.

LTV (First-Time-Buyer, Occupation). When assessing LTV for the risk of default the business intelligence rules consider the size of the deposit fronted by the borrower. In the event of a default, a high LTV indicates the borrower will suffer less of a loss compared to someone who has already invested a large amount of savings. In improving market conditions a FTB can expect to sell their house at a profit. A non-FTB with a high LTV may indicate poor financial management, or over stretching when trading up. Based on reputation, higher ranked Occupations are able to receive a higher LTV and should not be penalised as such.

House Value Group (LTV, MRTI). The greater the house value the less likely the borrower will default. Other factors to consider when assessing risk based on the house value is the size of the deposit paid by the borrower and the amount of income required to service the loan.

This section has described the methodology used to generate data and the process used to label the data. The risk score of a characteristic value is determined by coded business intelligence rules that have been devised based on consultations with a credit risk expert. The characteristic risk scores for an instance are then aggregated together to give a credit risk score for the instance. Based on a specified default rate, a cut-off score is determined whereby a percentage of the highest credit risk scores are assigned as defaulters. The business intelligence rules help to complicate the classification task by specifying non-linear interactions between the various characteristics.

5. Experimental Results

This section discusses the properties of a generated artificial dataset and illustrates the realistic nature of the artificial data. Using the conditional prior probabilities previously defined a dataset containing 3,000 instances is generated. An initial default rate of 3% is specified, along with a swap rate of 0.5% (i.e. the percentage of instances originally labelled Good but are re-assigned as Bad). This is an accurate approximation of the Irish default rate in 2007. The maximum affordability¹ is defined as 10, and the maximum MRTI is set at 90%. As a result, 119 (3.97%) instances are discarded as they exceed at least one of these values.

After the removal of unrealistic values, the dataset consists of 101 (3.51%) defaulters and 2780 (96.49%) repayers. As a starting point, a comparison between the artificial data and real-world data reported in Moody's (Moody's, 2010) is detailed in

¹outstanding loan amount divided by annual income

Table 18. This table indicates that the conditional prior probabilities of three of the characteristics (House Value Group, Loan Value Group, and LTV as it is used to calculate House Value) are reasonably accurate.

Table 18: Comparison of generated artificial data with real-world. House Value and Loan Value in '000.

Characteristic	Category	Artificial Data	Moody's
House Value Group	< 200	24%	17%
	200 - 400	52%	51%
	400 - 600	18%	18%
	600 - 800	4%	6%
	800 - 1,000	1%	3%
	> 1,000	1%	5%
Loan Value Group	< 200	40%	38%
	200 - 400	52%	49%
	400 - 600	6%	8%
	600 - 800	1%	2%
	800 - 1,000	1%	1%
	> 1,000	0%	2%

Tables 19 and 20 describe the distribution of the data for the borrower and loan demographics, respectively. Also reported are the weights of evidence (WoE) and information value (IV) for each of the categories. The WoE measures the predictive power of each category. The calculated value of the WoE is dependent on a binary outcome (i.e. good or bad). The WoE of a category is calculated as the logarithm of the ratio of the proportion of goods to the proportion of bads. In keeping with common practice the values have been multiplied by 100 in order to make the figures more readable. A large negative WoE value corresponds to a high risk of default, while a high positive value corresponds to a low risk.

Based on Table 19, the standard borrower demographics of a defaulter are likely to be: (i) a FTB (as per 75.2% of defaulters); (ii) less than 31 years of age (as per 59.4% of defaulters); (iii) earn less than 80,000 (as per 78.2% of defaulters); (iv) is employed in the Construction or Industry sectors (as per 56.4% of defaulters); (v) as an Occupation they are classed Farmer or Self-Employed (as per 36.6% of defaulters); (vi) they are likely to be part of either a 2 Adults, No child household or 1 Adult, no child < 18 household (as per 68.3% of defaulters); (vii) non-college educated, i.e. PB, LS, HS, or PLC (as per 67.3% of defaulters); and (viii) have an Expenses-to-Income ratio in the highest two quantiles (as per 83.1% of defaulters).

Based on Table 20, the standard loan demographics of a defaulter are likely to: (i) live in Other (as per 63.4% of defaulters); (ii) have a loan value of between 100,000 and 250,000 (as per 63.4% of defaulters); (iii) have a LTV of 0.93 or greater (as per 73.3% of defaulters); (iv) have a loan term of at least 35 years (as per 57.4% of defaulters); (v) have a Loan Rate based on either a standard variable or up-to-one-year fixed (as per 33.7% of defaulters); (vi) a house value of between 150,000 and 250,000 (as per 42.6% of defaulters); and (vii) have an MRTI ratio in the top two quantiles (as per 72.3% of defaulters).

The IV is used to assess the overall predictive strength of a characteristic. Table 21 provides the IV score for each characteristic. The characteristics are ordered based on their predictive strength with Income Group, Household Composition, and Occupation as the most predictive characteristics based on IV. Loan Rate, Loan Value Group, and Loan Term are deemed the weakest, this can be attributed in part to the removal of unrealistic values based on high affordability caused by large loan values. One would normally expect LTV and MRTI to be ranked higher, but again, as the more severe and unrealistic values are removed the predictive strength of the characteristics is weakened. Only 2.67% of the instances have an MRTI value greater than 33%.

Any characteristic with an IV score less than 0.02 should be rejected. An IV score above 0.3 and the characteristic is considered a strong predictor, and anything above 0.5 indicates the characteristic is over-predicting. As the described data is so imbalanced and artificially generated it is unsurprising that the IV scores are so large.

As an alternative approach, the user could generate 20,000 instances using the same default rate and swap rate. As before, unrealistic instances would be removed using a maximum affordability and MRTI rate. The user could then undersample the majority class to produce a balanced dataset.

Table 21: Information Value

Characteristic	IV
Income Group	1.94
Household Comp.	1.49
Occupation	1.45
Expenses-to-Income	1.20
Employment Sect	1.19
Education	1.15
LTV	0.84
FTB	0.78
MRTI	0.74
Age Group	0.51
Location	0.41
House Value Group	0.21
Loan Term	0.18
Loan Value Group	0.15
Loan Rate	0.10

6. Case Study: Population Drift

The following section examines the effects of population drift on the predictive performance of a classification model. This exercise also demonstrates the usefulness of our artificial data generation framework through the creation of datasets whose distributions gradually change over time.

6.1. Population Drift Background

Credit risk scorecards have a limited lifespan, and often their performance degrades over time. During scorecard construction samples drawn from data representative of the current population will rarely have the same distribution as those drawn

Table 19: Description of borrower demographics from generated dataset

Characteristic	Category	Count	Distrib.	#Good	Distrib. Good	#Bad	Distrib. Bad	WoE	IV
FTB	0	1899	65.9%	1874	67.4%	25	24.8%	100.19	0.43
	1	982	34.1%	906	32.6%	76	75.2%	-83.68	0.36
Age Group	18 - 25	251	8.7%	228	8.2%	23	22.8%	-102.12	0.15
	26 - 30	696	24.2%	659	23.7%	37	36.6%	-43.53	0.06
	31 - 35	654	22.7%	639	23.0%	15	14.9%	43.68	0.04
	36 - 40	488	16.9%	481	17.3%	7	6.9%	91.49	0.09
	41 - 45	329	11.4%	327	11.8%	2	2.0%	178.17	0.17
	46+	463	16.1%	446	16.0%	17	16.8%	-4.80	0.00
Income Group	40 - 60	222	7.7%	175	6.3%	47	46.5%	-200.04	0.80
	60 - 80	357	12.4%	325	11.7%	32	31.7%	-99.70	0.20
	80 - 100	440	15.3%	431	15.5%	9	8.9%	55.38	0.04
	100 - 120	411	14.3%	408	14.7%	3	3.0%	159.76	0.19
	120 - 150	600	20.8%	597	21.5%	3	3.0%	197.82	0.37
	150+	851	29.5%	844	30.4%	7	6.9%	147.72	0.35
Employment Sector	Agriculture, Forestry and fishing	149	5.2%	140	5.0%	9	8.9%	-57.07	0.02
	Construction	235	8.2%	205	7.4%	30	29.7%	-139.33	0.31
	Wholesale, Retail	410	14.2%	399	14.4%	11	10.9%	27.60	0.01
	Transportation, Storage	88	3.1%	86	3.1%	2	2.0%	44.61	0.00
	Hospitality	217	7.5%	214	7.7%	3	3.0%	95.23	0.05
	Information, Communication	162	5.6%	161	5.8%	1	1.0%	176.63	0.08
	Professional, Scientific, Technical	248	8.6%	246	8.8%	2	2.0%	149.71	0.10
	Admin., Support services	147	5.1%	144	5.2%	3	3.0%	55.61	0.01
	Public Admin.	147	5.1%	145	5.2%	2	2.0%	96.85	0.03
	Education	233	8.1%	232	8.3%	1	1.0%	213.17	0.16
	Health	282	9.8%	280	10.1%	2	2.0%	162.66	0.13
	Industry	241	8.4%	214	7.7%	27	26.7%	-124.49	0.24
	Financial	205	7.1%	202	7.3%	3	3.0%	89.46	0.04
	Other	117	4.1%	112	4.0%	5	5.0%	-20.60	0.00
Occupation	MAP	1224	42.5%	1216	43.7%	8	7.9%	170.88	0.61
	Office	697	24.2%	689	24.8%	8	7.9%	114.07	0.19
	Trade	403	14.0%	370	13.3%	33	32.7%	-89.81	0.17
	Manual Op.	147	5.1%	121	4.4%	26	25.7%	-177.74	0.38
	Farmer	116	4.0%	105	3.8%	11	10.9%	-105.90	0.08
	Self-Employed	294	10.2%	279	10.0%	15	14.9%	-39.19	0.02
Household Composition	1 Adult, no child < 18	491	17.0%	461	16.6%	30	29.7%	-58.29	0.08
	2 Adults, No child	203	7.0%	164	5.9%	39	38.6%	-187.88	0.61
	1 Adult, 1+ child < 18	763	26.5%	755	27.2%	8	7.9%	123.22	0.24
	2 Adults, 1+ child < 18	139	4.8%	136	4.9%	3	3.0%	49.90	0.01
	3 Adults, No child < 18	999	34.7%	993	35.7%	6	5.9%	179.39	0.53
	Other	286	9.9%	271	9.7%	15	14.9%	-42.10	0.02
Education	PB	72	2.5%	59	2.1%	13	12.9%	-180.25	0.19
	LS	99	3.4%	81	2.9%	18	17.8%	-181.10	0.27
	HS	151	5.2%	135	4.9%	16	15.8%	-118.24	0.13
	PLC	298	10.3%	277	10.0%	21	20.8%	-73.56	0.08
	TLND	824	28.6%	810	29.1%	14	13.9%	74.29	0.11
	TLHD	1354	47.0%	1338	48.1%	16	15.8%	111.13	0.36
	Other	83	2.9%	80	2.9%	3	3.0%	-3.17	0.00
Expenses-to-Income	1	595	20.7%	590	21.2%	5	5.0%	145.56	0.24
	2	599	20.8%	596	21.4%	3	3.0%	197.65	0.37
	3	588	20.4%	579	20.8%	9	8.9%	84.90	0.10
	4	568	19.7%	541	19.5%	27	26.7%	-31.75	0.02
	5	531	18.4%	474	17.1%	57	56.4%	-119.69	0.47

Table 20: Description of loan demographics from generated dataset

Characteristic	Category	Count	Distrib.	#Good	Distrib. Good	#Bad	Distrib. Bad	WoE	IV
Location	Dublin	908	31.5%	898	32.3%	10	9.9%	118.25	0.26
	Cork	442	15.3%	426	15.3%	16	15.8%	-3.32	0.00
	Galway	200	6.9%	194	7.0%	6	5.9%	16.10	0.00
	Limerick	118	4.1%	116	4.2%	2	2.0%	74.54	0.02
	Waterford	86	3.0%	83	3.0%	3	3.0%	0.51	0.00
	Other	1127	39.1%	1063	38.2%	64	63.4%	-50.51	0.13
Loan Value Group	< 100	240	8.3%	238	8.6%	2	2.0%	146.40	0.10
	100 - 150	340	11.8%	328	11.8%	12	11.9%	-0.70	0.00
	150 - 200	567	19.7%	543	19.5%	24	23.8%	-19.60	0.01
	200 - 250	579	20.1%	551	19.8%	28	27.7%	-33.56	0.03
	250 - 300	477	16.6%	462	16.6%	15	14.9%	11.24	0.00
	300 - 400	460	16.0%	445	16.0%	15	14.9%	7.49	0.00
	400+	218	7.6%	213	7.7%	5	5.0%	43.68	0.01
LTV	0.45	81	2.8%	81	2.9%	0	0.0%	n/a	n/a
	0.55	131	4.5%	129	4.6%	2	2.0%	85.16	0.02
	0.6	204	7.1%	203	7.3%	1	1.0%	199.81	0.13
	0.65	276	9.6%	275	9.9%	1	1.0%	230.17	0.20
	0.7	325	11.3%	319	11.5%	6	5.9%	65.83	0.04
	0.75	349	12.1%	345	12.4%	4	4.0%	114.22	0.10
	0.85	466	16.2%	453	16.3%	13	12.9%	23.59	0.01
	0.93	601	20.9%	570	20.5%	31	30.7%	-40.34	0.04
	0.975	115	4.0%	104	3.7%	11	10.9%	-106.86	0.08
1	333	11.6%	301	10.8%	32	31.7%	-107.37	0.22	
Loan Term	20	411	14.3%	398	14.3%	13	12.9%	10.64	0.00
	25	804	27.9%	786	28.3%	18	17.8%	46.15	0.05
	30	571	19.8%	559	20.1%	12	11.9%	52.62	0.04
	35	972	33.7%	921	33.1%	51	50.5%	-42.15	0.07
	40	123	4.3%	116	4.2%	7	6.9%	-50.74	0.01
Loan Rate	Fixed - Over 5 years	1275	44.3%	1240	44.6%	35	34.7%	25.24	0.03
	Tracker Type 1	457	15.9%	437	15.7%	20	19.8%	-23.09	0.01
	Tracker Type 2	281	9.8%	274	9.9%	7	6.9%	35.21	0.01
	Standard Variable	437	15.2%	417	15.0%	20	19.8%	-27.77	0.01
	Up to 1 year fixed	238	8.3%	224	8.1%	14	13.9%	-54.25	0.03
Fixed - 3 to 5 years	193	6.7%	188	6.8%	5	5.0%	31.19	0.01	
House Value Group	< 150	375	13.0%	362	13.0%	13	12.9%	1.16	0.00
	150 - 200	331	11.5%	311	11.2%	20	19.8%	-57.10	0.05
	200 - 250	470	16.3%	447	16.1%	23	22.8%	-34.80	0.02
	250 - 300	430	14.9%	416	15.0%	14	13.9%	7.65	0.00
	300 - 350	370	12.8%	357	12.8%	13	12.9%	-0.23	0.00
	350 - 400	250	8.7%	242	8.7%	8	7.9%	9.44	0.00
	400 - 500	346	12.0%	339	12.2%	7	6.9%	56.50	0.03
500+	309	10.7%	306	11.0%	3	3.0%	130.99	0.11	
MRTI	1	600	20.8%	593	21.3%	7	6.9%	112.42	0.16
	2	600	20.8%	588	21.2%	12	11.9%	57.67	0.05
	3	600	20.8%	591	21.3%	9	8.9%	86.95	0.11
	4	600	20.8%	578	20.8%	22	21.8%	-4.66	0.00
	5	481	16.7%	430	15.5%	51	50.5%	-118.31	0.41

from the future population. Such differences may arise out of changes in macro-economic conditions, company strategy, and personal circumstances (Hoadley, 2001). When one data source S_1 changes to another S_2 , *concept drift* is said to have occurred (Žliobaitė, 2009).

Gao *et al.* (2007) formalise and categorise concept drift in a given feature vector x and an associated class label y as changes in the joint probability $P(x, y) = P(y|x) \cdot P(x)$. Where $P(x)$ represents feature probability and $P(y|x)$ the class label conditional probability. Changes in either two of these components determine the category of concept drift as:

1. Feature change: $P(x)$ changes but $P(y|x)$ remains the same.
2. Conditional change: $P(x)$ remains the same but $P(y|x)$ changes.
3. Dual change: Both $P(x)$ and $P(y|x)$ change.

It should be noted that in the literature there are many definitions and categorisations of concept drift. For example, Narasimhamurthy and Kuncheva (2007) highlight that the term *population drift* is frequently used to describe changes in the underlying distributions of the data, which is analogous to the Gao *et al.* (2007) description of *feature change*. Population drift is also referred to as *covariate shift* (Shimodaira, 2000) or *sample selection bias* (Huang *et al.*, 2007b), however the last term relates more so to the acquisition of training sample data. In this work we use the term population drift.

The ability to correctly detect when a concept begins to drift along with a strategy to derive the necessary information required to handle changing concepts is essential in the study of domains with changing context (Mak and Krause, 2006). Changes in the underlying population pose a serious problem in practical fields such as finance, medical diagnosis or bioinformatics (Hand, 2006a). In the banking domain, because of its competitive environment, this problem is particularly acute (Hand, 2006a). Failure to recognise population drift can result in major strategic risks, as it implies that the tools used to motivate decisions may have unseen faults.

As scoring models typically only use data on loans that have reached maturity, credit scoring models are frequently constructed from data which is out-of-date. The data used involves sampling loan applicants from a selected period of time, referred to as the *sampling window*. The performance of the applicants is then observed over the next k months, referred to as the *performance window*. In order for the loans to mature, Gayler (2006) recommends that a performance window of at least 12 months is required. As loans typically default over an extended period after the loan has been granted, this allows a reasonable proportion of such loans to default. In addition to this, time must be added in order to collect observations that account for seasonal variations in the applicant population. Before the scorecard becomes operational further time is required for steps such as data preparation, data modelling and implementation (Gayler, 2006). Retail loans typically mature between three-to-five years (Siddiqi, 2005). After implementation, the model may then be in use for some time - normally

three years, but more than five years is not unknown (Gayler, 2006). Even if the applicant population distribution is stationary this may still be a problem as lenders may alter their systems and procedures at any time which may result in random variations in the data collecting process (Gayler, 2006).

In the rest of this section we describe an exercise we performed to demonstrate the usefulness of the artificial data generation. Population drift is introduced into the data and its impact on the predictive performance of a classifier is examined.

6.2. Population Drift Evaluation

The aims of this evaluation described are to examine the robustness of the logistic regression (logit) classifier in the presence of population drift. This is achieved by comparing the performance of a trained logit model on: (i) a batch of artificially generated data whose conditional prior probabilities have been adjusted in order to produce population drift; and (ii) a batch of artificially generated data whose conditional prior probabilities remain static, and as such does not experience any significant population drift. Logit is selected as it is the most commonly used classification model in credit scoring. The logit model was implemented using the Weka (version 3.7.1) machine learning framework (Witten and Frank, 2000). The ridge estimator parameter was optimised in order to offset unstable coefficient estimates that arise from highly correlated data.

6.3. Data

The data is generated using the previously described artificial data framework. The datasets used in the evaluation consist of 2,000 instances. A default rate of 2.5% (50 instances) is specified along with a swap rate of 0.33% (6 instances). A noise value from a normal distribution with a standard deviation of 0.5 is applied to the credit risk score of each instance. Instances with an MRTI greater than 90% or an affordability equal to or greater than 10 are removed. Depending on the conditional prior probabilities this typically accounts for 2% - 4.5% of the data. To ensure reproducibility of the contents of this paper, we have provided access to all of the data and developed techniques used in this article at the author's homepage².

6.4. Performance Measures

Two evaluation measures are used in this study: the geometric mean and the area under the receiver operator curve (AUC). The geometric mean measures classification performance at a specific classification threshold, whereas the AUC assesses classifier performance over a distribution of costs. No tests are performed to determine statistically significant differences in classifier performance. The purpose of the artificial data is to examine the basic assumptions of population drift - that classifier performance degrades as data changes.

²http://www.comp.dit.ie/aigroup/?page_id=101

6.4.1. Geometric Mean

Classifier output is typically binary: 1 for accepting (*non-defaulter*) or 0 for rejecting (*defaulter*) a credit applicant. Many ranking classifiers also produce a numeric score which can be binarised by the use of a threshold. The threshold determines true positive (TP), true negative (TN), false positive (FP) (classified as positive, but actually negative) and false negative (FN) (classified as negative, but actually positive) counts for a given test set. We use *sensitivity* and *specificity*, as used by Baesens *et al.* (2003), to measure the classification quality of all classifiers used in our study. Sensitivity is calculated as: $\frac{TP}{TP+FN}$ and measures the proportion of positive (repayer) examples that are predicted to be positive. Specificity, calculated as: $\frac{TN}{TN+FP}$, measures the proportion of negative (defaulter) examples that are predicted to be negative. As per Kubat and Matwin (1997), in order to provide a suitable composite measure of sensitivity and specificity we employ the *geometric mean*, which is calculated as shown in Equation 1.

$$\text{Geometric Mean} = \sqrt{\text{Sensitivity} * \text{Specificity}} \quad (1)$$

The geometric mean calculation used assumes equal misclassification costs for both false positive and false negative predictions. This may be a problem if we consider that one type of classification error may be a lot more costly than the other. However, in the absence of available cost matrices the geometric mean is the most appropriate performance criteria as a means of assessing the accuracy of a classifier at a specific threshold.

6.4.2. AUC

The AUC is commonly used in credit scoring to estimate the performance of classification algorithms in the absence of information on the cost of different error types. The AUC represents the performance of a classifier over all possible cost ratios.

6.5. Methodology

A dataset was generated based on the settings described in Section 6.3. The dataset used was divided into two subsets: (i) the training set (70%); and (ii) the validation set (30%). The training set and the validation set were used to train and tune the logit classifier. In the next step, in order to create a control benchmark, a total of 15 datasets are generated. These datasets use the same conditional prior probabilities and settings as the training data. The default rate of the generated datasets is determined by the cut-off score derived from the training data. The performance of the logit model was verified using the 15 non-drift datasets. As no population drift is simulated, we label the datasets the *non-drift* datasets.

We conduct a second set of experiments using the same training and validation dataset. The cut-off score from the training dataset is used to set the default rate in the subsequent datasets. To simulate population drift the conditional prior probabilities of the following characteristics are adjusted: (i) Location; (ii) New House; (iii) FTB; (iv) Age Group; (v) Occupation; (vi) Employment Sector; (vii) Education; (viii) Expenses. This adjustment occurs over 5 phases. For the first phase, the conditional prior probabilities remain unchanged. During each

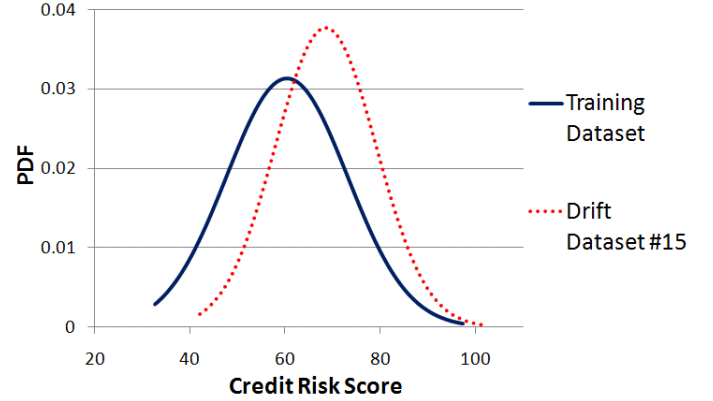


Figure 2: Probability density function (PDF) of the training dataset and the final population drift dataset

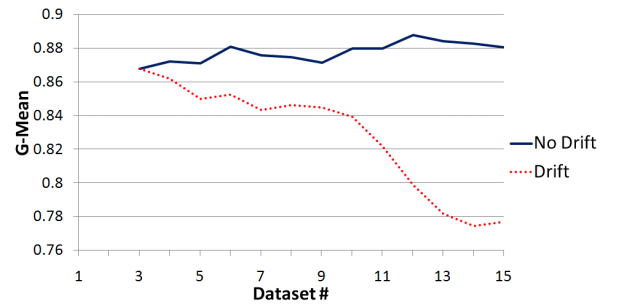


Figure 3: Geometric mean (G-Mean) of logistic regression on drift and non-drift datasets, based on a moving average over 3 datasets

phase three artificial datasets are generated, in total 15 artificial datasets are produced in addition to the training dataset. Figure 2 illustrates the change in the credit risk scores between the training dataset to the final drift dataset (dataset #15). The adjustment to conditional prior probabilities of the aforementioned characteristics has caused a rise in the credit risk scores and ultimately the number of defaulters.

Each experiment was conducted 20 times using different randomly selected training, and validation set splits and the results reported are averages of these 20 runs.

6.6. Results

It can be seen from Figure 3 and Figure 4 that the relative performance of the logit model does not hold constant on data with population drift. As the AUC is broad measure of classifier performance the difference in performance of the logit model on both batches of data is still apparent, but not as pronounced as the geometric mean.

The individual differences between the performance of the logit model on the drift and non-drift data, along with the corresponding default rates is displayed in Table 22. At the beginning of the fourth phase, marked by dataset number 10, the performance of the logit model on the Drift data displays a marked decline in comparison to its performance on the Control data. This is most likely caused by the jump in the number of defaulters (3.94% to 4.96%), as the logit model was trained using

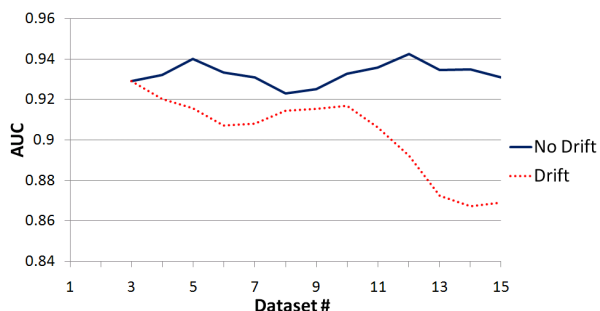


Figure 4: AUC of logistic regression on drift and non-drift datasets, based on a moving average over 3 datasets

a relatively low number of defaulters. We conjecture that as the number of defaulters increase the performance of the logit model on Drift data will continue to decline.

Table 22: Geometric mean evaluated on Control and Drift datasets. The default rate for each dataset is also displayed.

Dataset #	G-Mean		Defaulter %	
	Control	Drift	Control	Drift
1	0.873	0.873	3.33%	3.33%
2	0.884	0.884	2.80%	2.80%
3	0.846	0.846	2.95%	2.95%
4	0.885	0.855	3.13%	2.87%
5	0.882	0.848	3.02%	3.79%
6	0.876	0.855	2.65%	3.31%
7	0.870	0.828	2.68%	4.16%
8	0.879	0.857	2.70%	3.67%
9	0.865	0.851	3.13%	3.94%
10	0.895	0.811	3.32%	4.96%
11	0.879	0.804	3.32%	4.36%
12	0.889	0.782	3.00%	4.62%
13	0.885	0.760	3.52%	4.66%
14	0.874	0.783	2.75%	5.78%
15	0.884	0.789	3.22%	5.11%

This section presented a case study on population drift and has demonstrated, through the use of artificial data, the effects of population drift on classifier performance.

7. Conclusions

In this work we have described the impediments researchers encounter when attempting to obtain real-world data. Often legal requirements and commercial sensitivities prevent the sharing of data amongst the research community, particularly in credit scoring. It is our hope that this discussion will lead to greater understanding and awareness of the issue. Furthermore, we have outlined the benefits of sharing data amongst researchers to help impress upon the key stakeholders within financial institutions to enable and reward data sharing within the credit risk community.

Quite often access to real-world data is facilitated by machine learning repositories. Although such repositories serve

several important functions and over time they may evolve to include a greater collection of credit scoring datasets, they do not allow for controlled experimentation (Japkowicz and Shah, 2011). The primary advantage artificial data holds over real-world data is the ability for researchers to design experiments under which certain conditions and parameters can be accurately controlled.

The main focus of this study was to propose a framework to generate artificial data that can be used to simulate credit risk scenarios. We have developed an artificial dataset reflecting the Irish mortgage market from 2007 based on available statistics and expert opinion. The ability to adjust the conditional prior probabilities of the characteristics allow users to generate realistic datasets with which to assess the behaviour of classification techniques. The label application was performed based on extensive consultations with a credit risk expert with whom business intelligence rules were devised that generate non-linear distributions based on interactions between the characteristics.

As per Japkowicz and Shah (2011), we are of the opinion that artificial data should not be used to assess the superiority of one classification method over another. Artificial data cannot be expected to replicate the rich structural complexities of real-world data. It can, however, assist researchers in decisions about research direction and design. For example, we demonstrate how the artificial data framework can be used to show the effects of population drift on the performance of a logistic regression model.

We made several assumptions in the coding of our business intelligence rules, for future work some of these assumptions may be reconsidered. The next stage of our research currently being undertaken involves assessing the impact of population drift on classifier performance using a real-world dataset obtained from an Irish financial institution. Analysis of the real-world data will be used to further refine the artificial data.

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